

# Dynamic Nuclear Polarisation (Continuous Wave)

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# Menu

## Starter

DNP in a nutshell

## Main Course

Trio of DNP mechanisms:  
Solid effect, Overhauser Effect, and Cross Effect

## Dessert

A selection of experimental details

The saying goes, there are three problems with NMR...

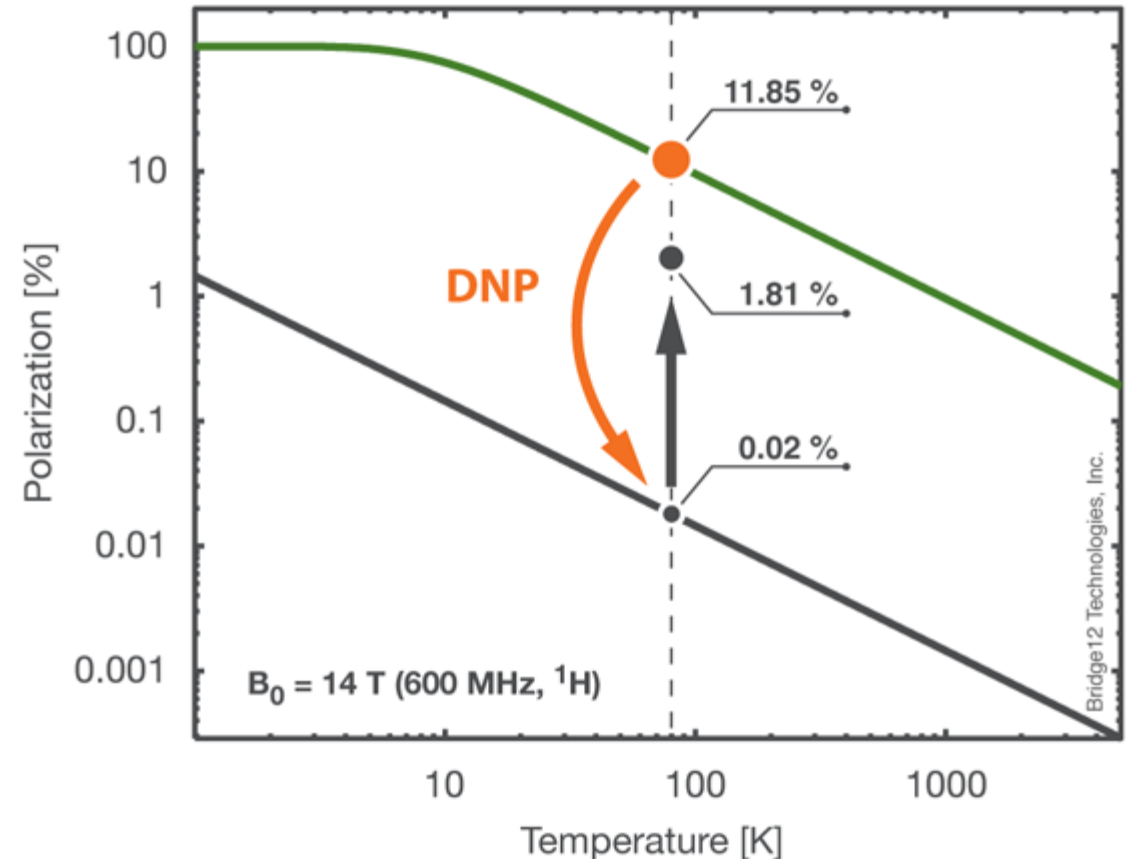
...sensitivity, sensitivity, and sensitivity!

-Various sources

# NMR Signal $\propto$ Spin Polarisation

$$P = \tanh\left(\frac{\hbar\gamma B_0}{2k_B T}\right) \approx \frac{\hbar\gamma B_0}{2k_B T}$$

- $^1\text{H}$  at 600 MHz, 100 K:  
 $P = 0.02\%$
- $\gamma_e = 658 \gamma_H$ ,  $P = 12\%$
- DNP: transfer polarisation from electrons to nuclei!



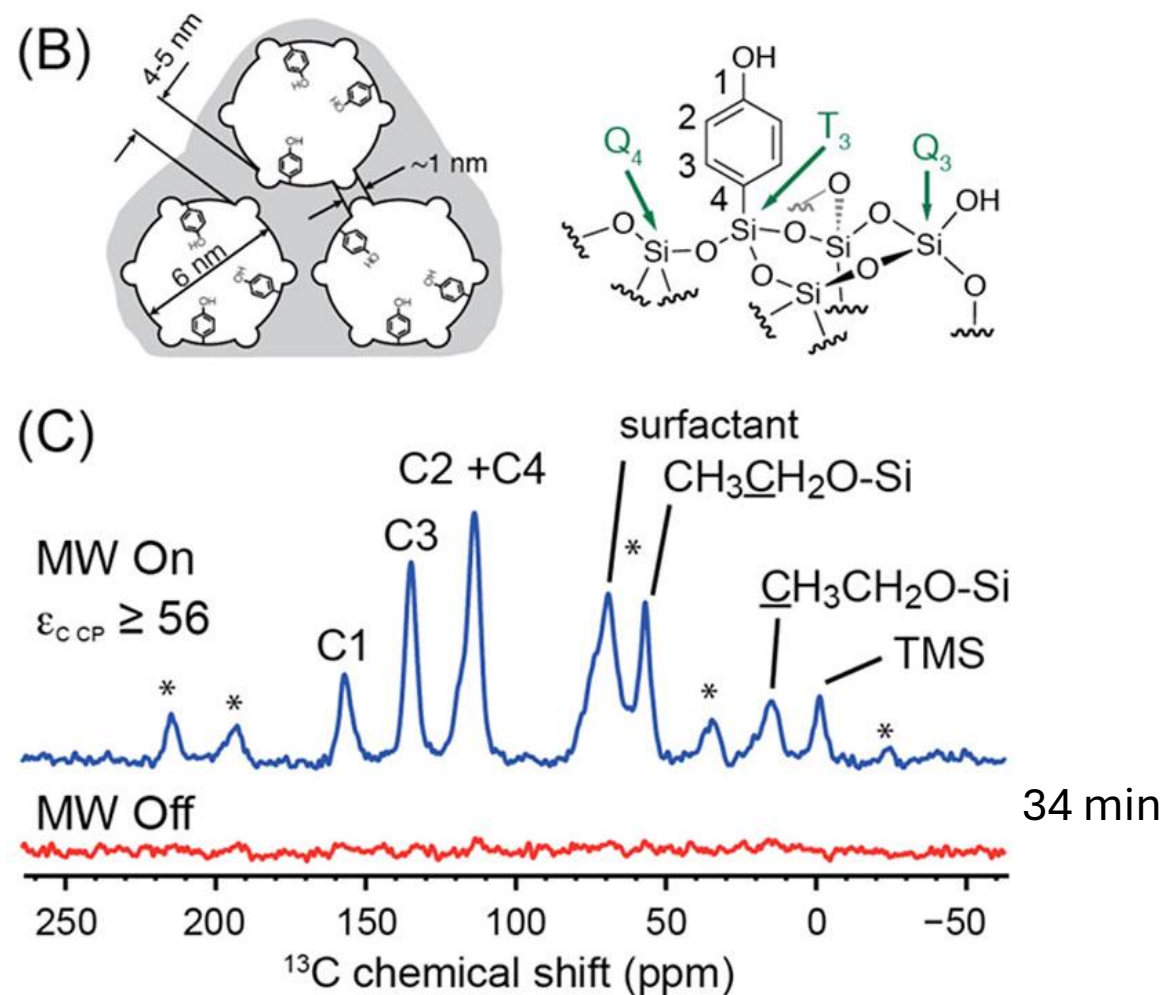
# An Example

DNP enable experiments that would be impractically long otherwise

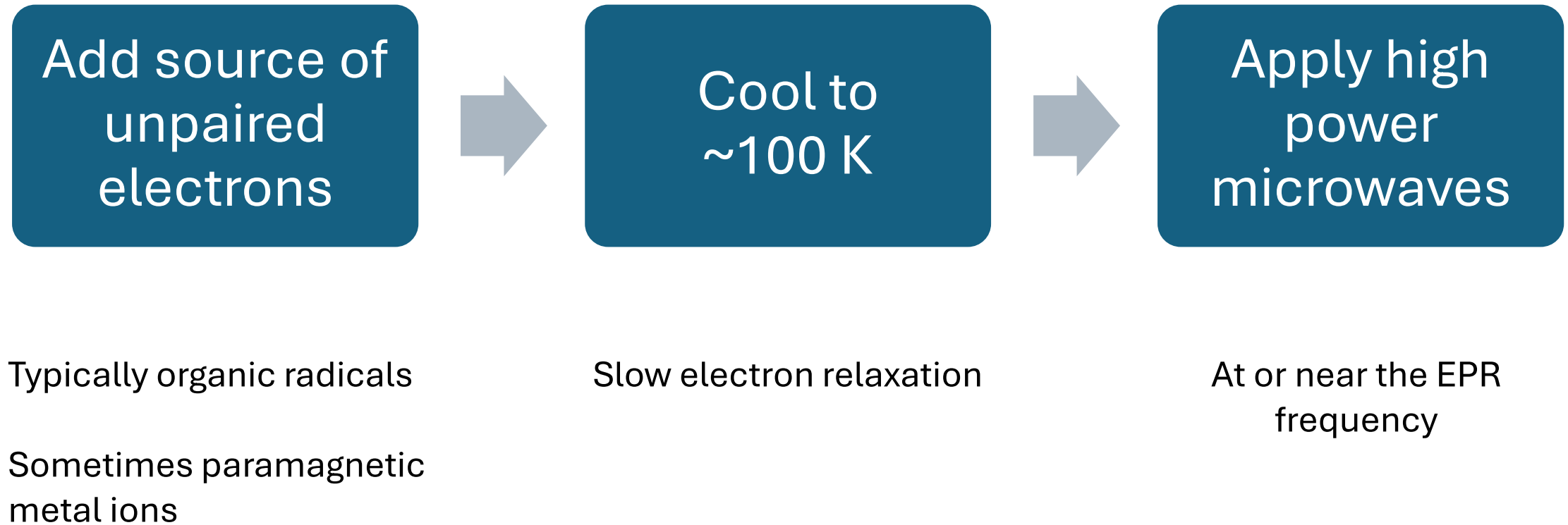
E.g. natural abundance  $^{13}\text{C}$  of low concentration organic species on silica surfaces

Enhancement,  $\varepsilon = I_{\text{ON}}/I_{\text{OFF}}$

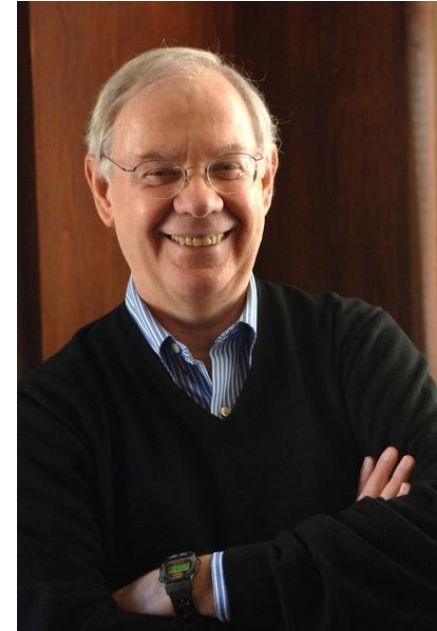
(>3000× time saving)



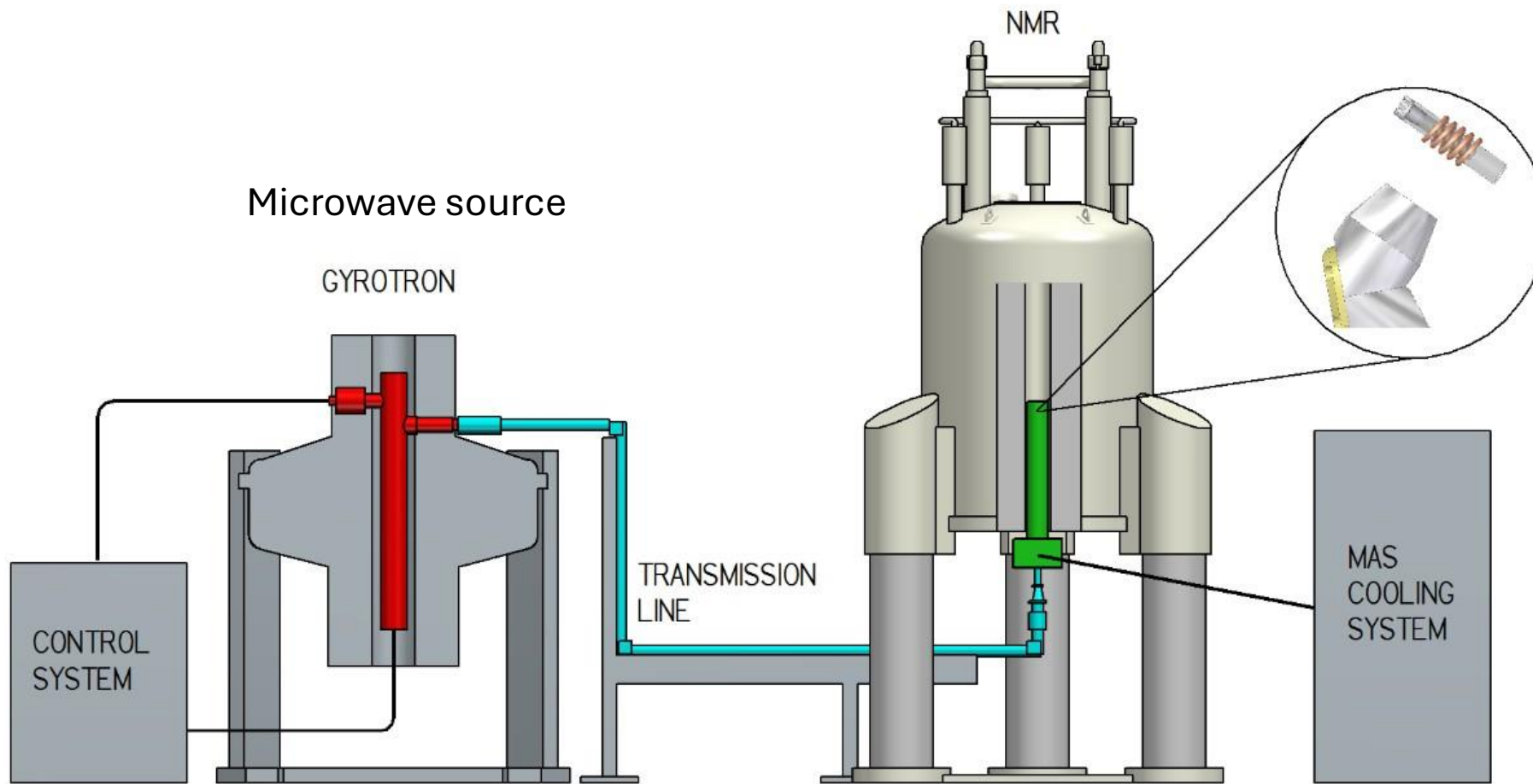
# DNP 101



# DNP instrumentation



Bob Griffin  
MIT



MAS at  $\sim 100$  K

# DNP instrumentation

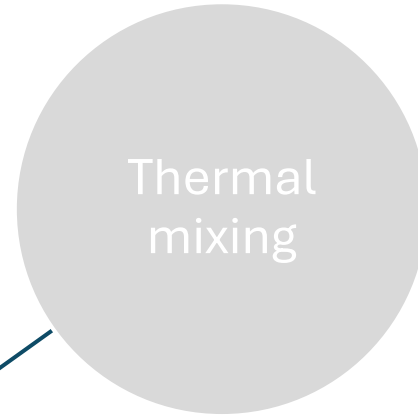
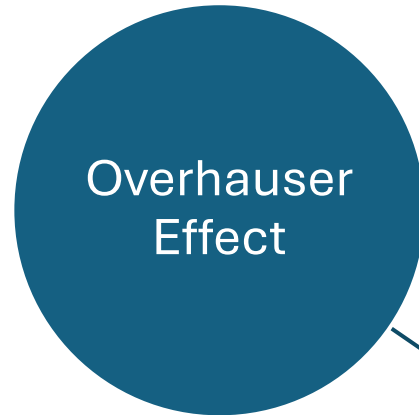


University of Nottingham DNP MAS NMR Facility, UK

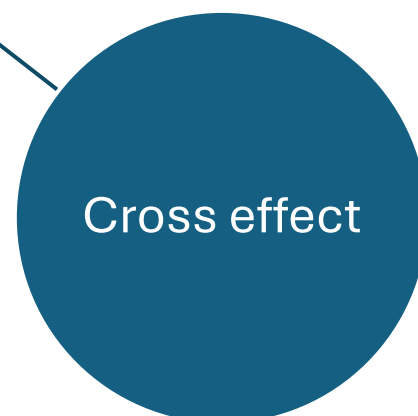
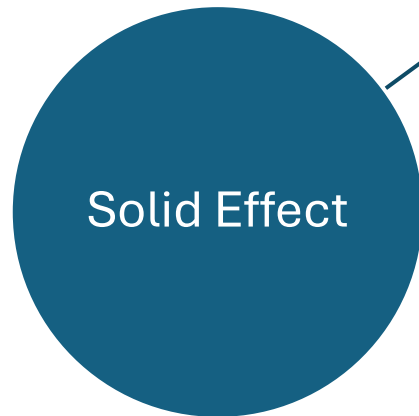
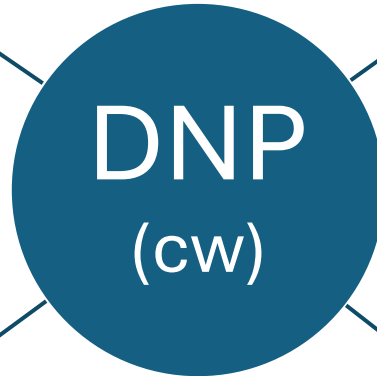


# How to transfer polarisation?

- First example of DNP
- Now mainly liquids

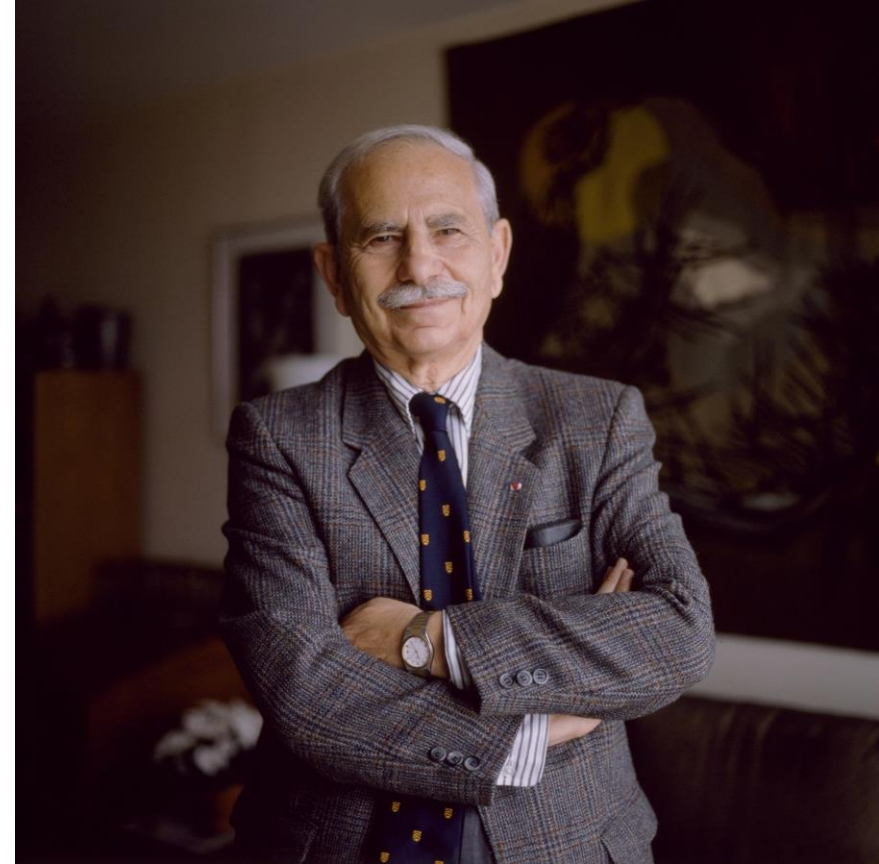


- High conc. of radicals
- Low T (<10 K)



- Most common for MAS DNP!

# Solid Effect

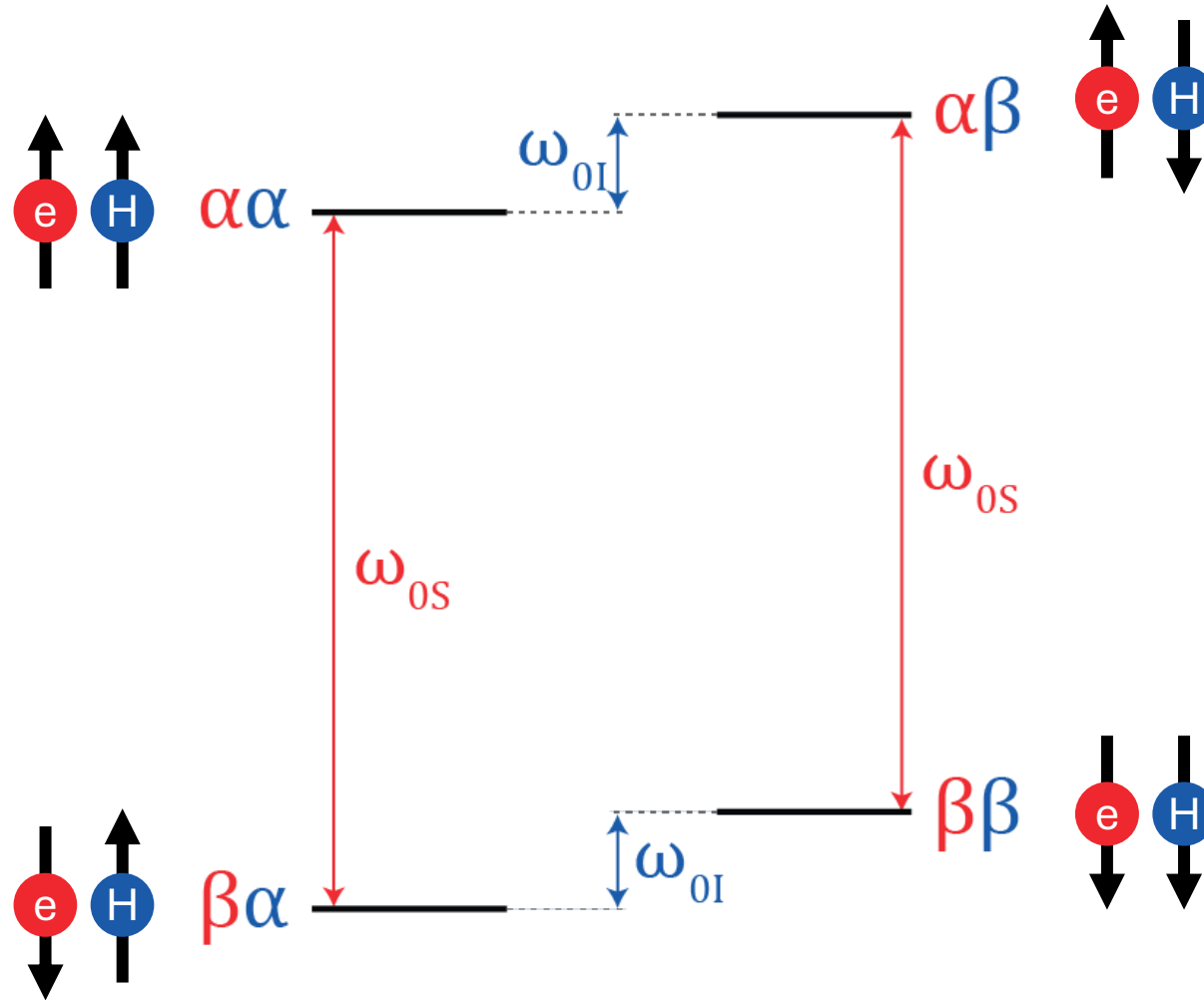


Anatole Abragam

# The electron-nuclear two-level system

$\alpha$  = spin up  
 $\beta$  = spin down

E  

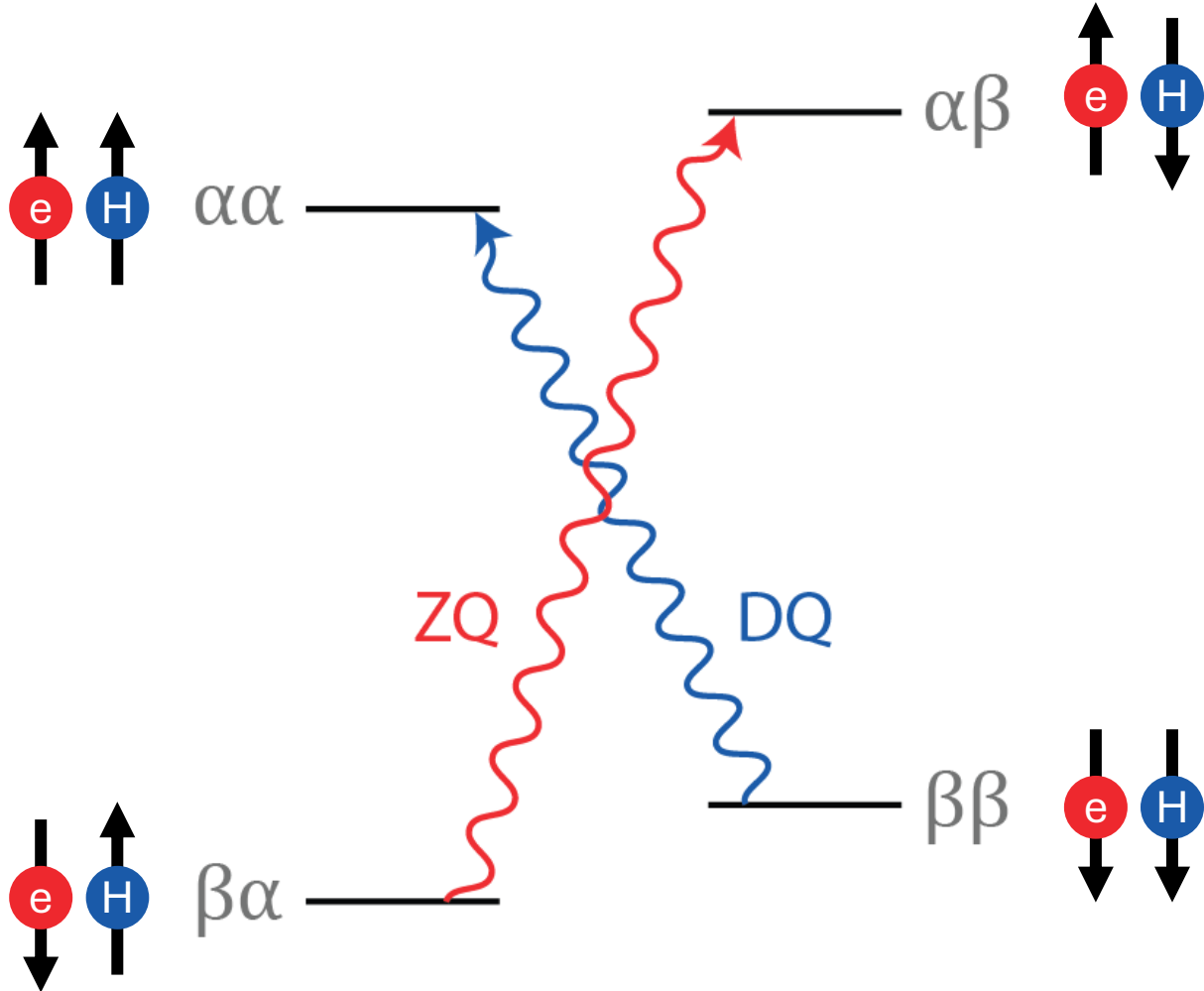



Note:  $\gamma_e$  is negative!

$$\Psi = |m_S m_I\rangle$$

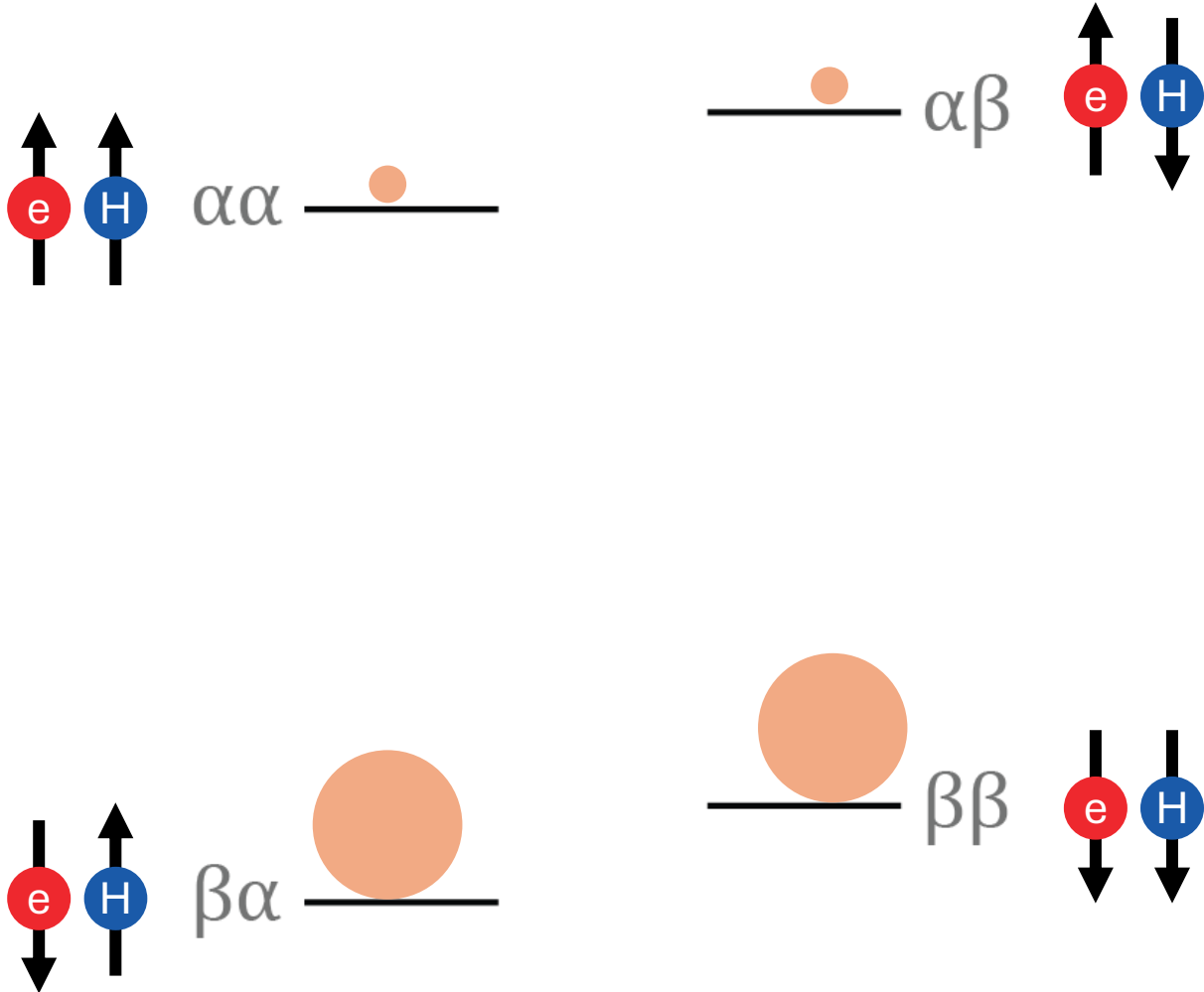
electron                      nucleus

# Solid Effect: ZQ and DQ transitions



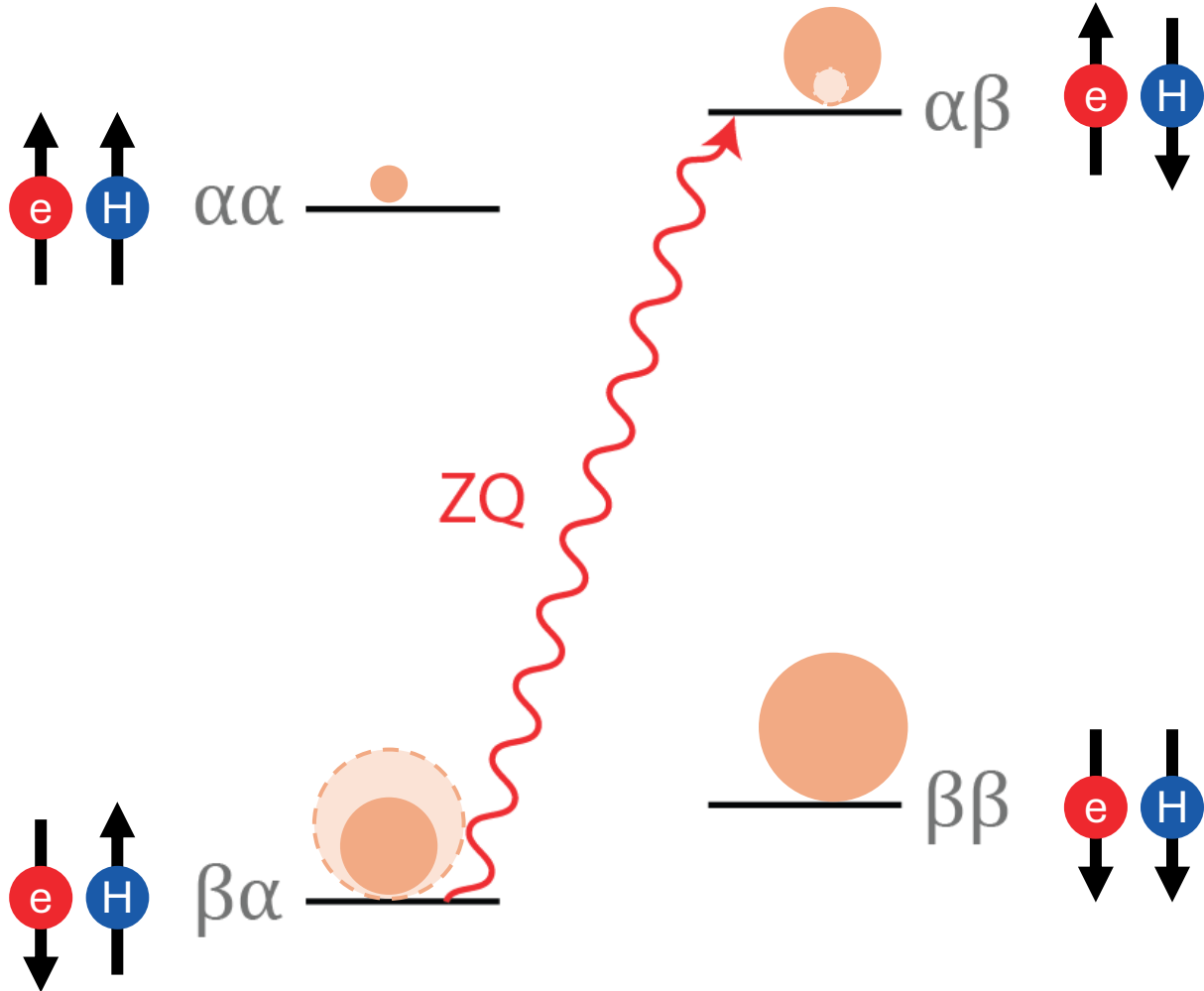
- **ZQ** = zero quantum
- **DQ** = double quantum
- Simultaneously flip electron and nuclear spin

# Solid Effect: Populations



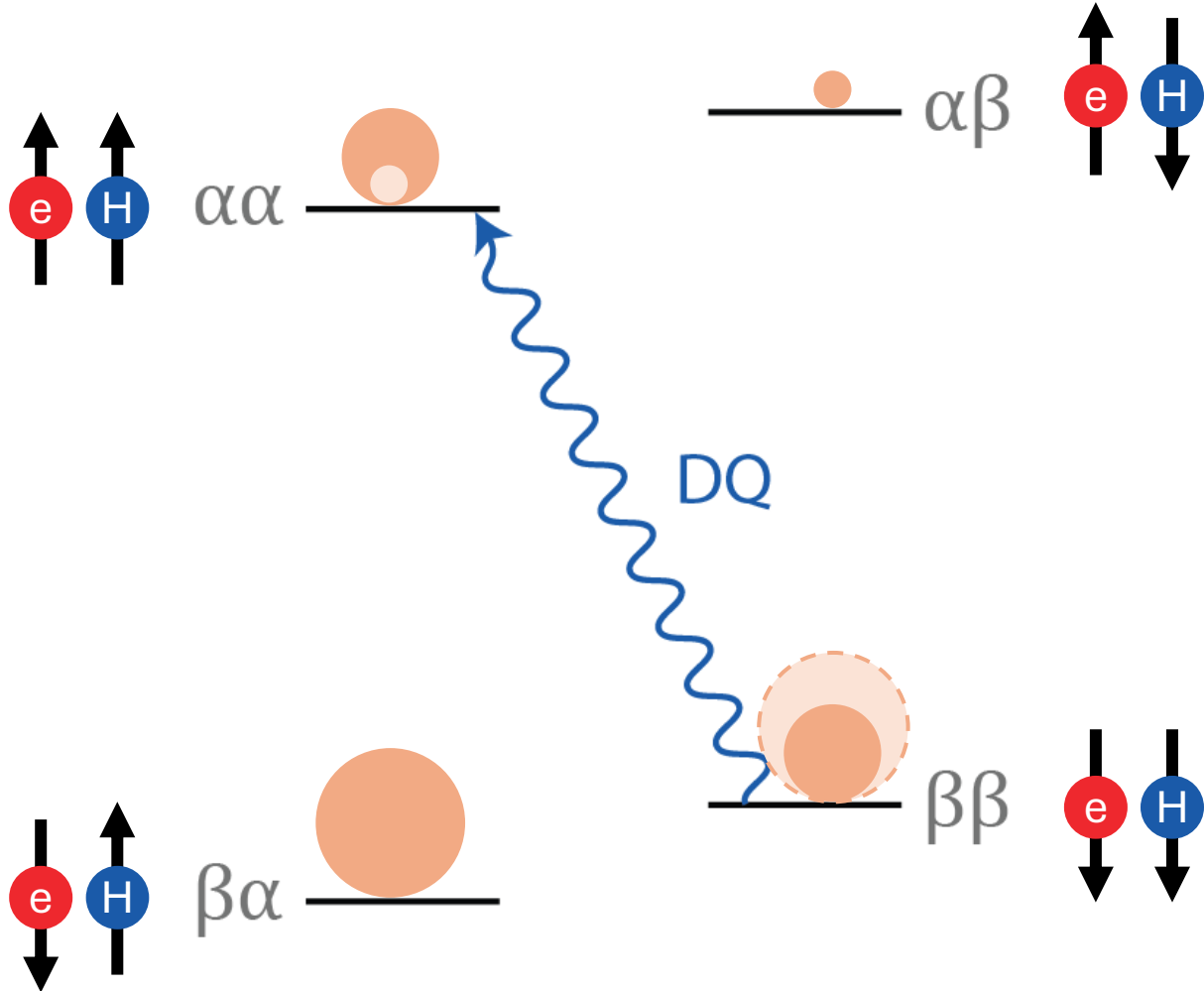
- Thermal equilibrium
- Electron spin polarisation: big (population difference)
- Nuclear spin polarisation: small (similar population)

# Solid Effect: Saturating ZQ Transition



- CW microwaves act to equilibrate the populations
- **Electron spin polarisation: reduced**
- **Nuclear spin polarisation: large negative enhancement**

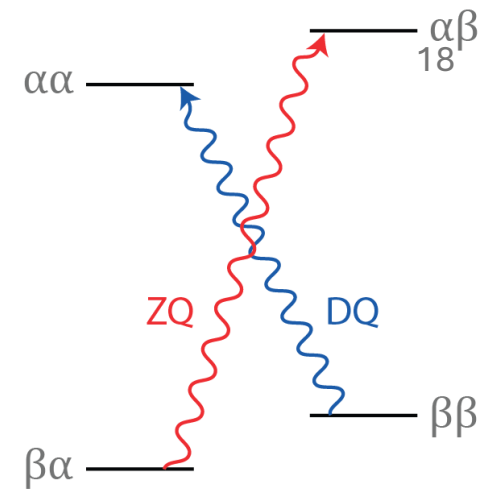
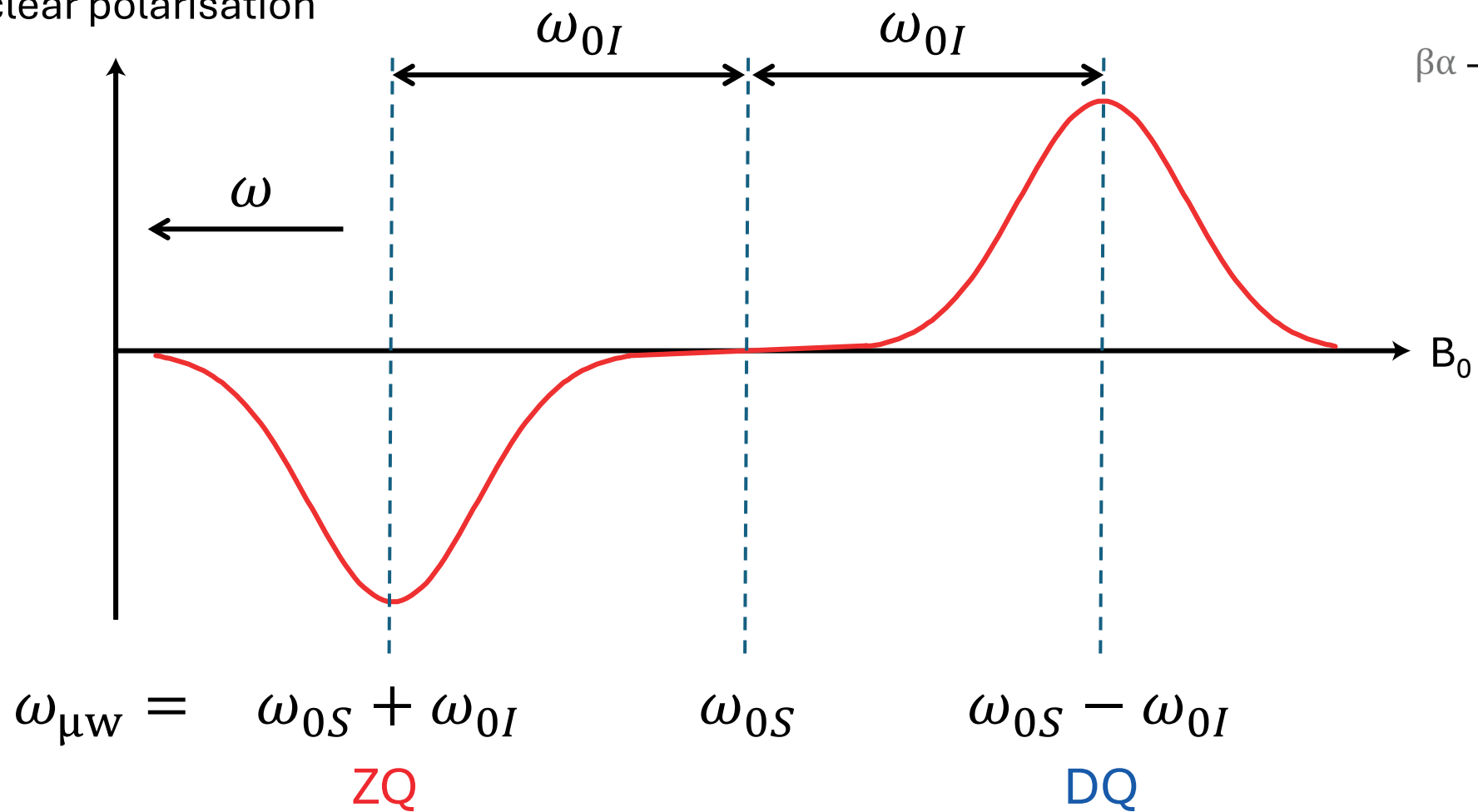
# Solid Effect: Saturating DQ Transition



- CW microwaves act to equilibrate the populations
- **Electron spin polarisation: reduced**
- Nuclear spin polarisation: large positive enhancement

# Solid effect: Field Profile

Nuclear polarisation





But wait...

multiple quantum transitions are forbidden!

Let's look at some maths

# Pseudosecular coupling

- $\hat{H}_I = -\omega_{0I}\hat{I}_z + \hat{\mathbf{S}} \cdot \mathbb{A} \cdot \hat{\mathbf{I}}$
- $\hat{H}_I = -\omega_{0I}\hat{I}_z + A_{zz}\hat{S}_z\hat{I}_z + A_{zx}\hat{S}_z\hat{I}_x$
- $\hat{H}_I = -\omega_{0I}\hat{I}_z + A\hat{S}_z\hat{I}_z + B\hat{S}_z\hat{I}_x$
- $A = \text{secular coupling}$
- $B = \sqrt{A_{zx}^2 + A_{zy}^2}$  (in general)  
“Pseudosecular coupling”

$$\hat{\mathbf{S}} = \begin{pmatrix} 0 \\ 0 \\ \hat{S}_z \end{pmatrix}$$

$$\hat{\mathbf{I}} = \begin{pmatrix} \hat{I}_x \\ \hat{I}_y \\ \hat{I}_z \end{pmatrix}$$

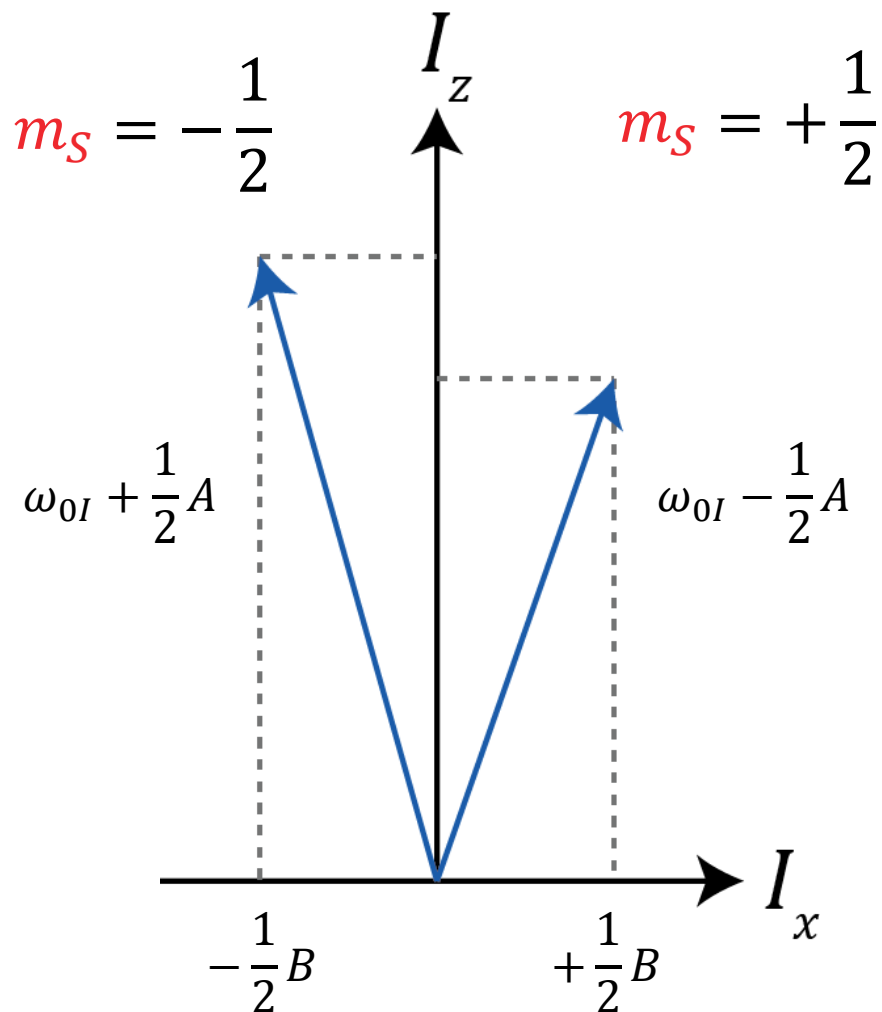
$$\mathbb{A} = \begin{pmatrix} A_{xx} & 0 & A_{xz} \\ 0 & A_{yy} & 0 \\ A_{zx} & 0 & A_{zz} \end{pmatrix}$$

Electron.  
Zeeman dominates,  
aligned with  $B_0$  ( $z$ )  
(secular approx. for  $S$ )

Nucleus.  
Hyperfine coupling  
perturbs. Can't assume  
aligned with  $z$

Hyperfine coupling.  
Assume electron and  
nucleus in  $xz$  plane

# Tilting of axis of quantisation



$$\hat{H}_I = (-\omega_{0I} + A\hat{S}_z)\hat{I}_z + B\hat{S}_z\hat{I}_x$$

$$\hat{S}_z\psi = m_S\psi = \pm\frac{1}{2}\psi$$

- Quantisation axis is tilted away from  $z$  (equivalent to mixing of  $\alpha$  and  $\beta$ )
- Orientation depends on the electron spin state

Electron State	Nuclear Eigenstates
$\alpha$	$\alpha + \delta\beta$ $\beta - \delta\alpha$
$\beta$	$\alpha - \delta\beta$ $\beta + \delta\alpha$

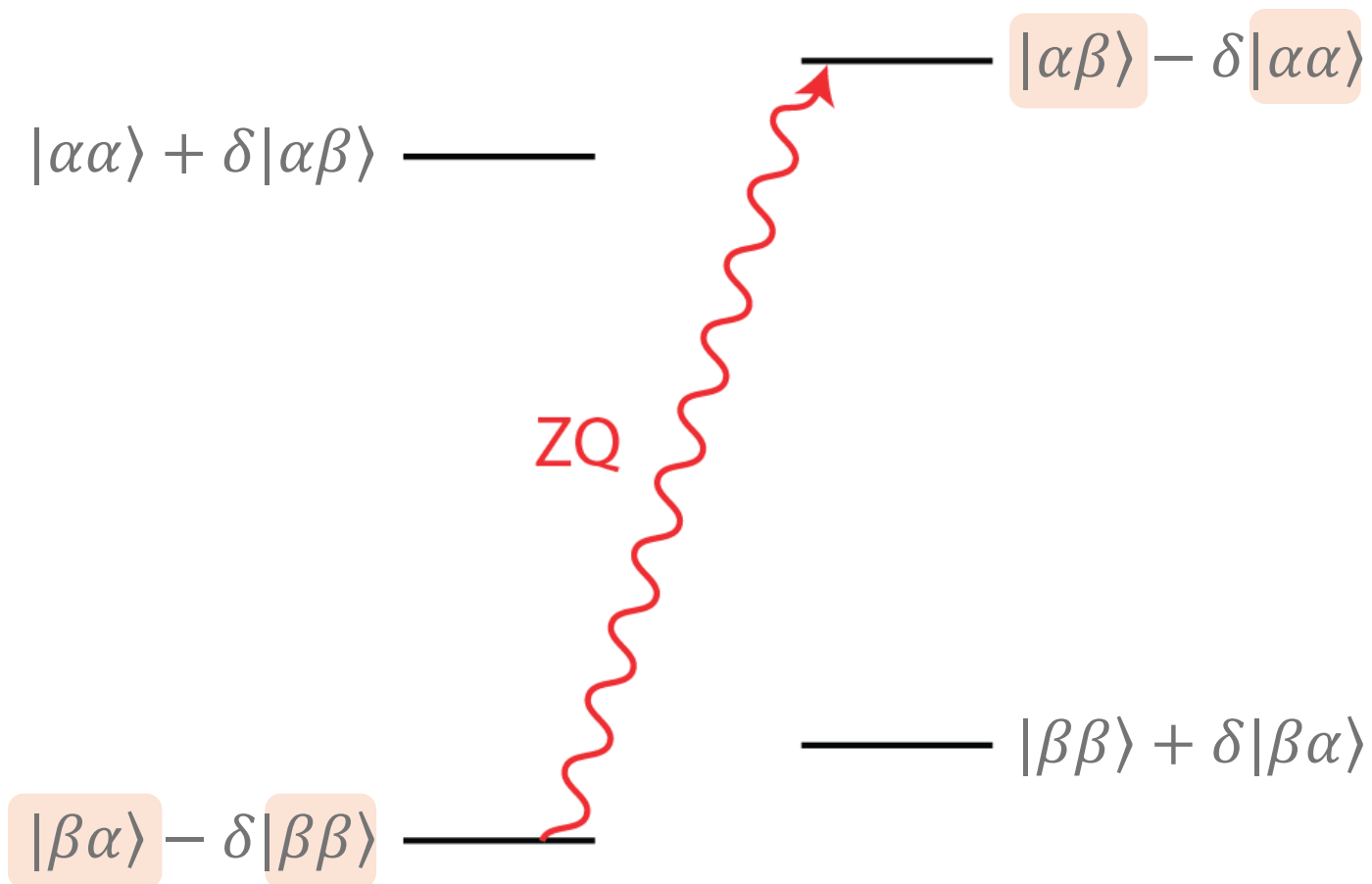
High field limit:

$$\delta = \frac{B}{4\omega_{0I}} < 1\%$$

# State mixing enables transitions

$$\begin{array}{ccc}
 & & \text{————— } |\alpha\beta\rangle - \delta|\alpha\alpha\rangle \\
 |\alpha\alpha\rangle + \delta|\alpha\beta\rangle & \text{—————} & \\
 & & \\
 & & \text{————— } |\beta\beta\rangle + \delta|\beta\alpha\rangle \\
 |\beta\alpha\rangle - \delta|\beta\beta\rangle & \text{—————} &
 \end{array}$$

# State mixing enables transitions



- Transitions are allowed between the mixed-in states
- Overall the transitions become weakly allowed, depending on the size of the pseudosecular coupling

$$\delta = \frac{B}{4\omega_{0I}}$$

- Pseudosecular coupling requires anisotropic e-n coupling. Not possible in (isotropic) liquids!

# What limits the enhancement?

Enhancement is determined by how efficiently we can saturate the ZQ or DQ transition.

Strength of e-n pseudosecular hyperfine coupling vs.  $\omega_0$   
Short e-n distance, lower  $B_0$

$$\varepsilon \propto \delta^2 \propto \frac{A_{zx}^2}{\omega_{0I}^2} \propto \frac{1}{B_0^2}$$

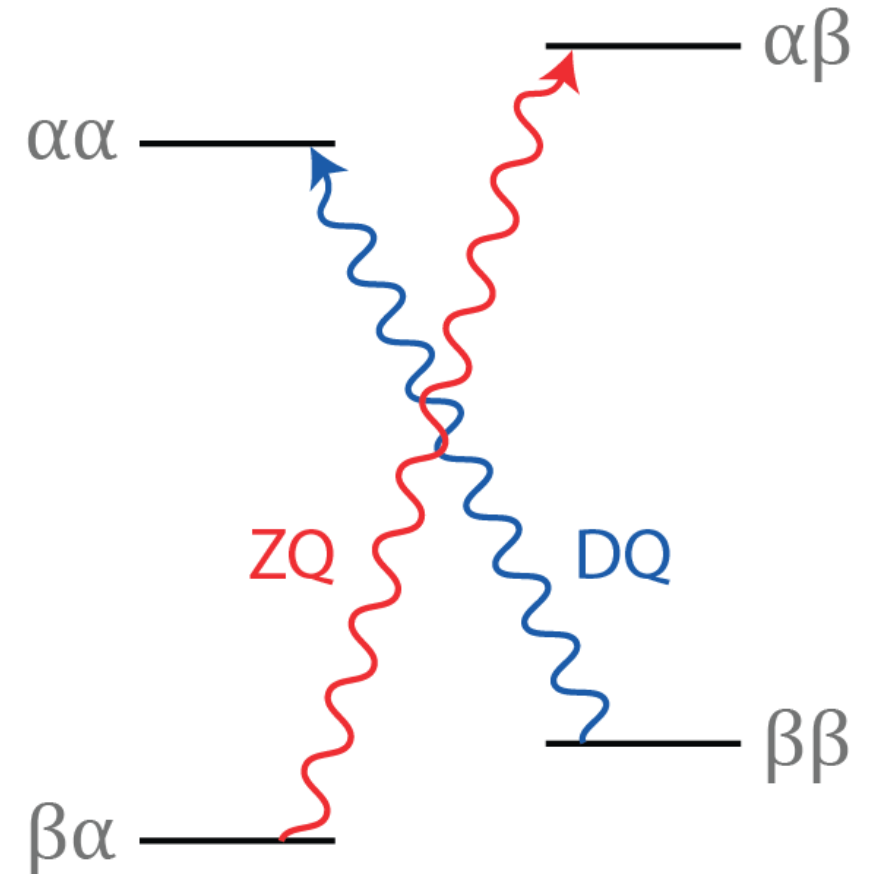
EPR linewidth and relaxation.  
Narrow line and long  $T_{1e}$  easier to saturate

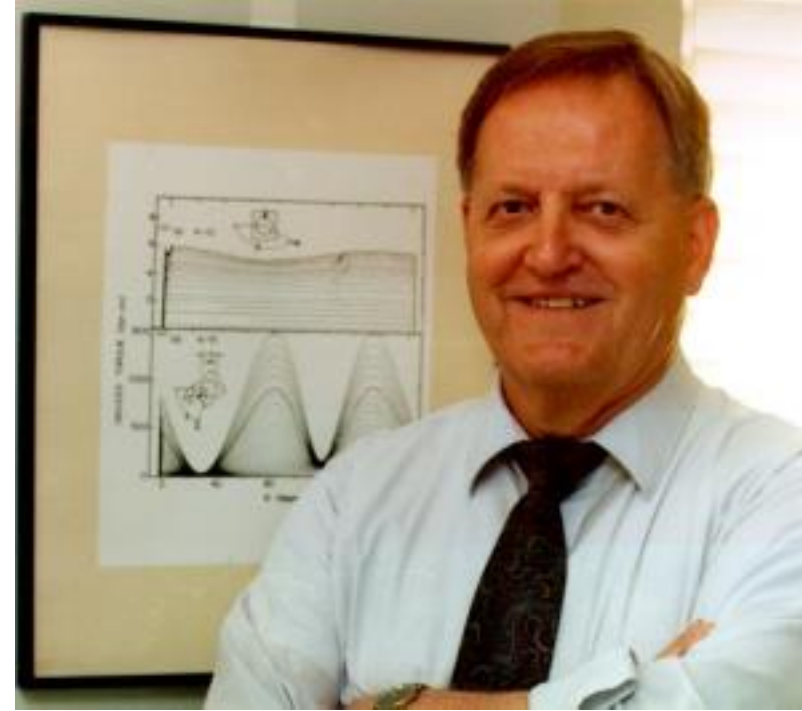
Microwave power. Transitions are only weakly allowed  
so typically need high microwave powers

# Summary: Solid Effect

- Microwaves drive ZQ or DQ transitions in e-n two spin system
- Simultaneously flip both spins. Transfer polarisation from electron to nucleus
- Requires anisotropic e-n coupling. Not possible in isotropic liquids

Questions?





# Overhauser Effect

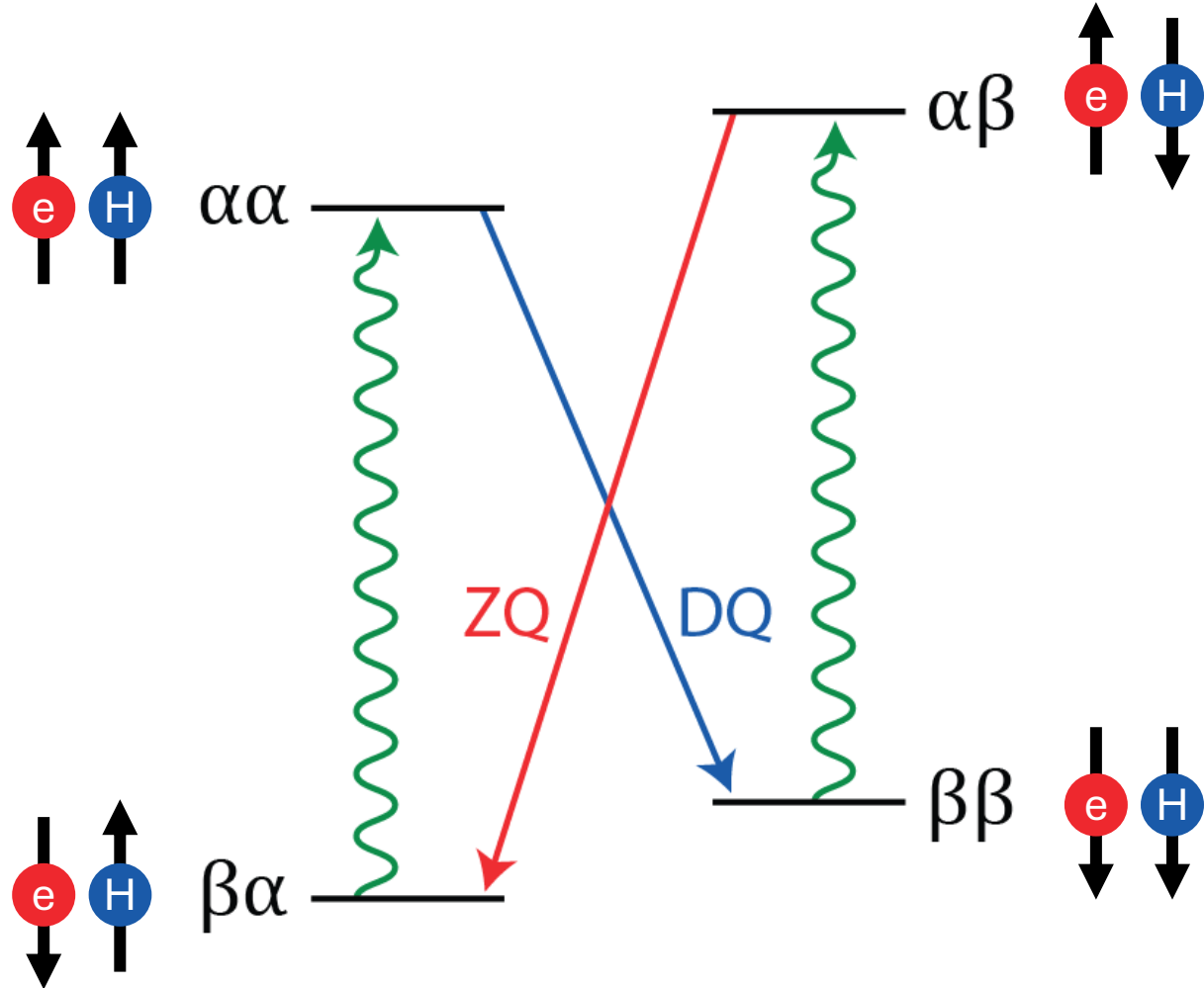
“The discovery of dynamic nuclear polarisation took me two days”

-Albert Overhauser

(Experimental proof by Carver and Slichter in 1953 took about 9 months)

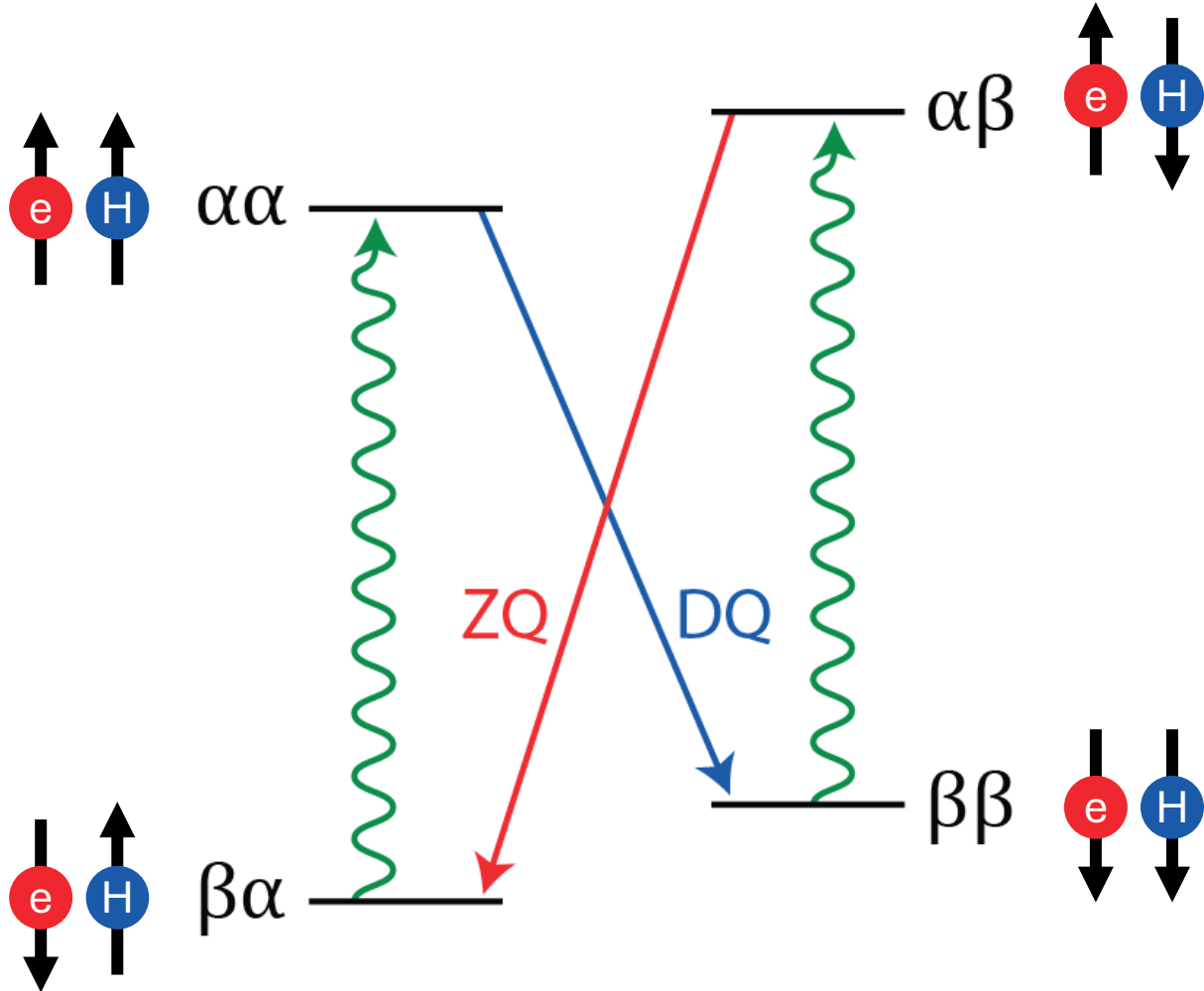


# Overhauser Effect



- Saturate allowed single quantum transitions with microwaves
- Cross-relaxation generates nuclear hyperpolarisation
- If ZQ and DQ rates are different

# Overhauser Effect Enhancement Sign



- Sign of OE enhancement depends whether **ZQ** or **DQ** relaxation dominates

**ZQ** > **DQ**

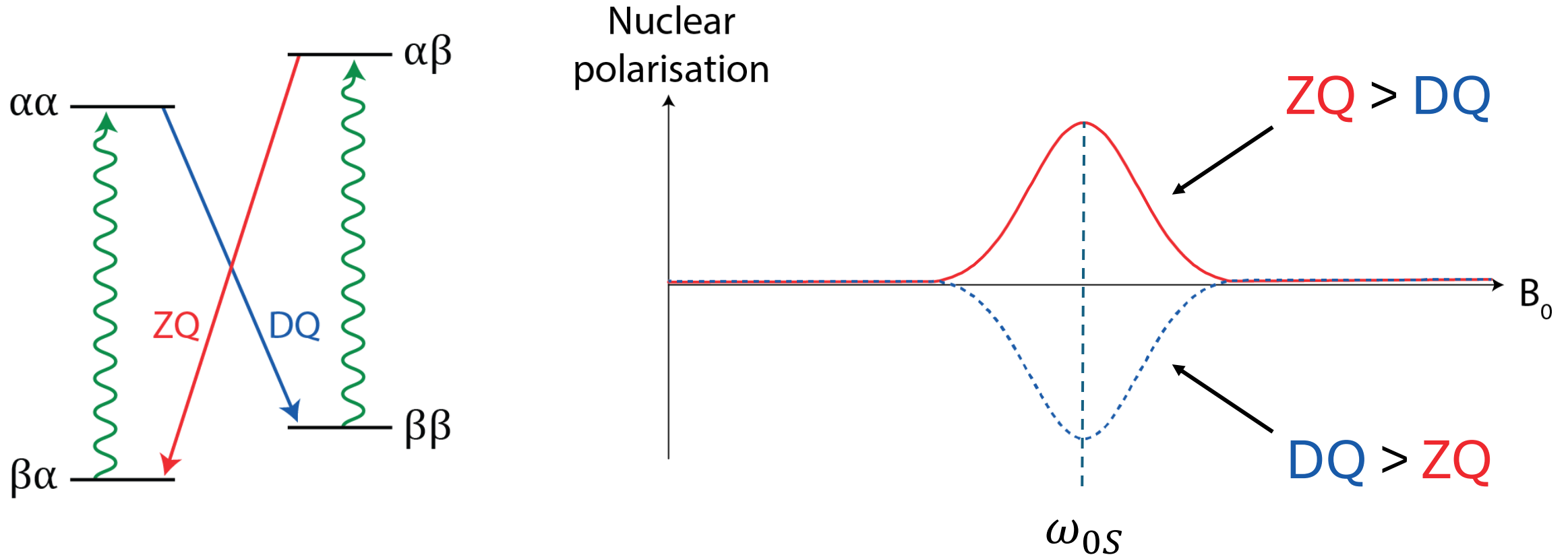
Positive  $\varepsilon$

**DQ** > **ZQ**

Negative  $\varepsilon$

- Unlike SE, we can't choose the sign!

# Overhauser Effect Field Profile



What determines relaxation rates?

# Solomon Theory

- Cross relaxation is driven by fluctuations in the hyperfine coupling at around the EPR frequency
- Hyperfine coupling can have scalar (Fermi contact) and/or dipolar components:  $\mathbb{A} = A^{\text{FC}} + \mathbb{A}^{\text{dip}}$



Ionel Solomon

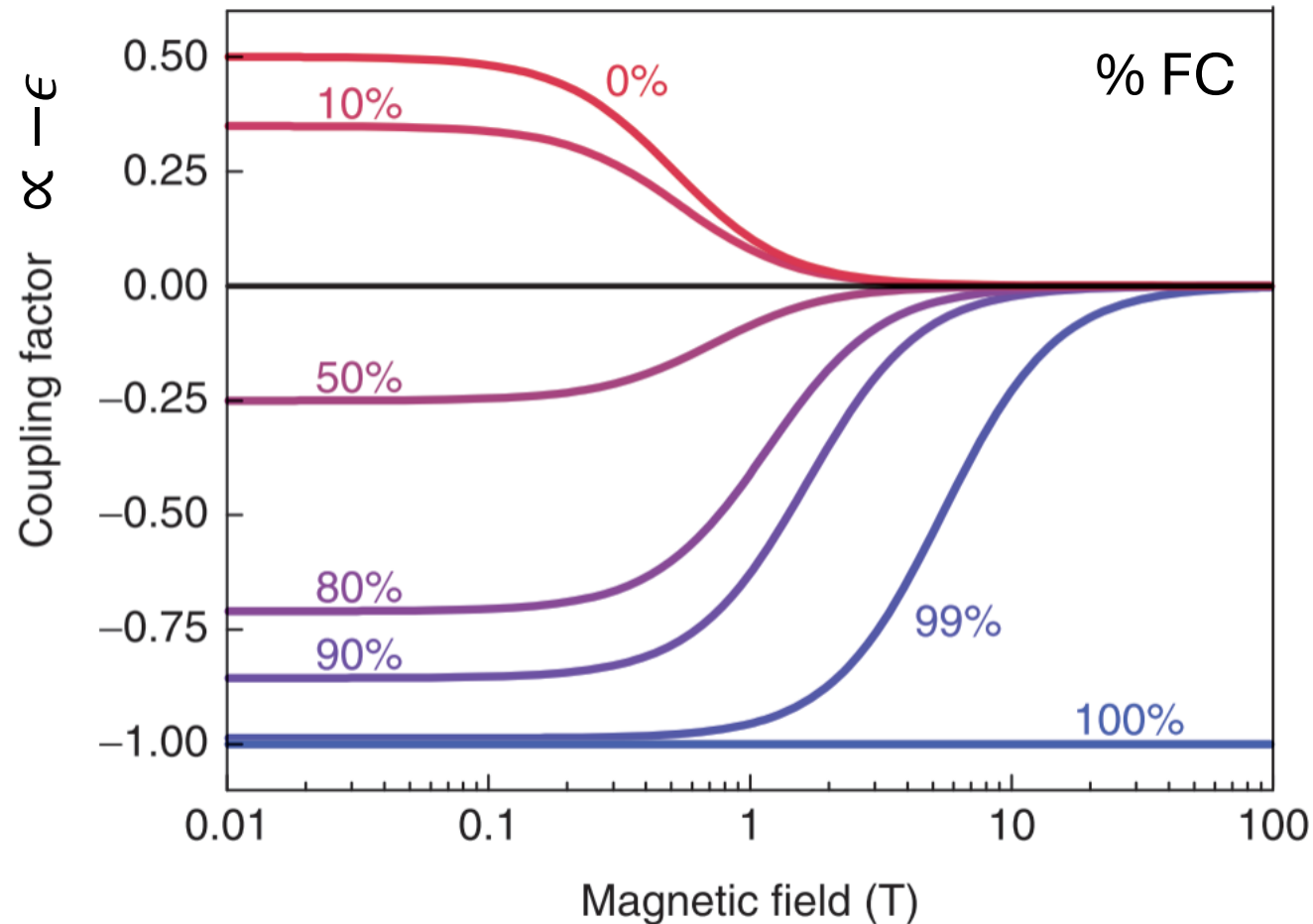
## Fermi Contact

- Only **ZQ** relaxation possible
- Positive enhancement

## Dipolar Coupling

- **DQ** > **ZQ**
- Negative enhancement
- Above ~1 T, SQ nuclear relaxation is too fast: no enhancement!

# Overhauser Effect Field Dependence

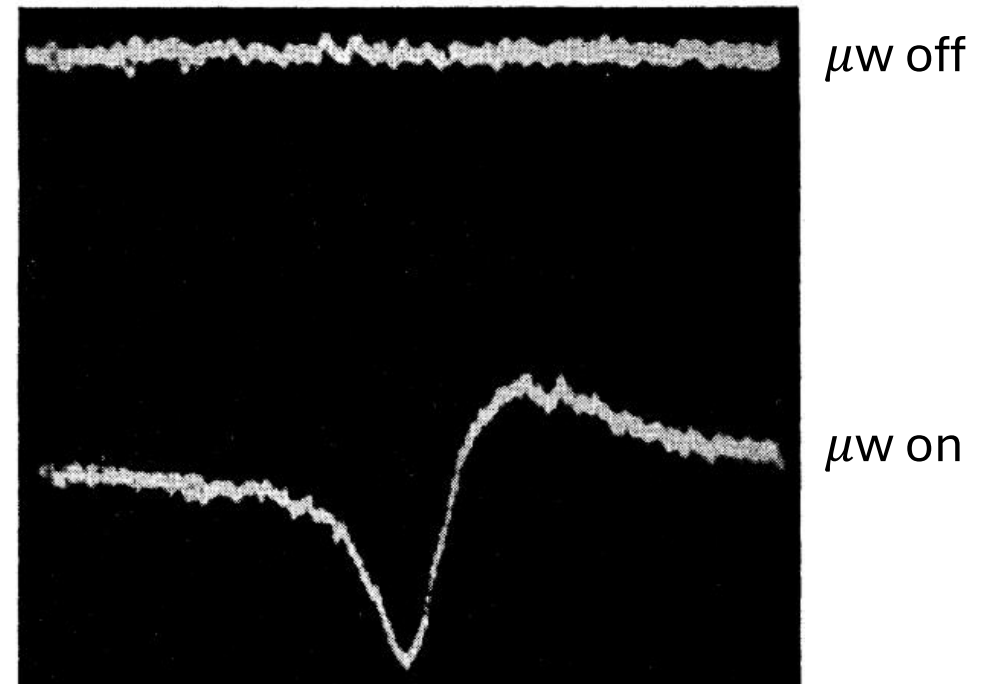


- Pure Fermi Contact:  
Positive enhancement
- Dipolar coupling:  
Negative enhancement,  
only at low field
- Any dipolar contribution  
eventually kills OE

# Overhauser Effect in Metals

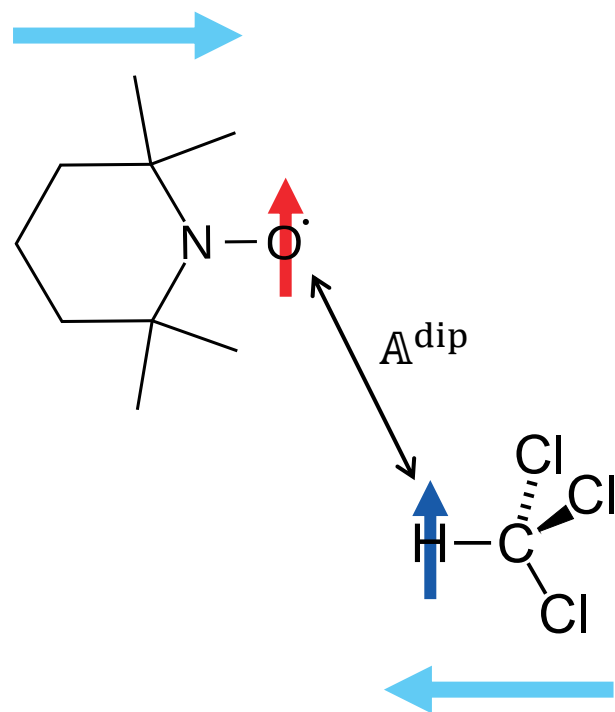
- In metals, fluctuations are caused by fast moving conduction electrons
- Electrons at the Fermi level have a velocity of  $\sim 1 \times 10^6$  m/s
- Fermi contact dominates

$^7\text{Li}$  NMR of Li Metal



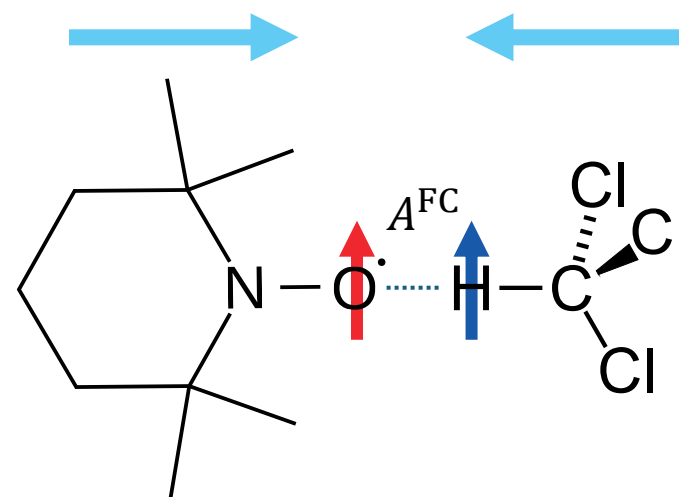
# Hyperfine fluctuations in solution

e.g. TEMPO in chloroform



Dipolar coupling

Modulated by relative molecular diffusion



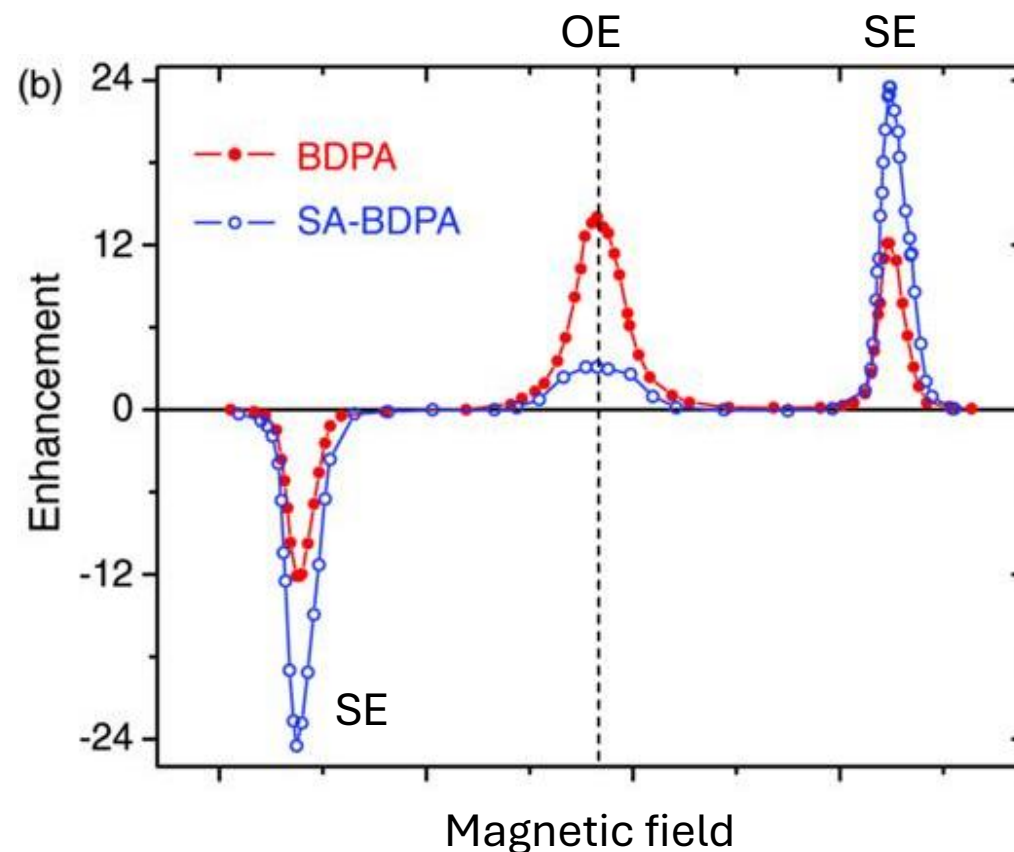
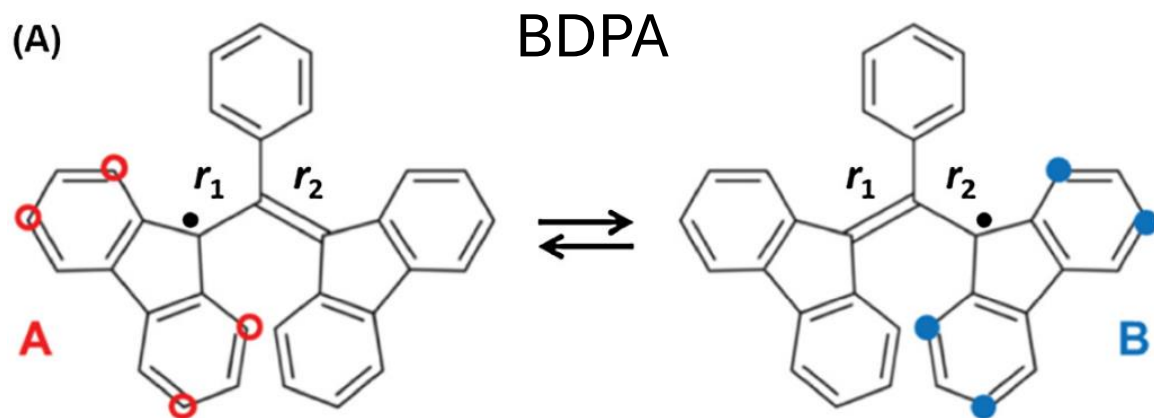
Scalar coupling

Modulated by molecular collisions

- Both FC and dipolar.  $^1\text{H}$  only works at low field.  $^{13}\text{C}$  has less dipolar so works at 9.4 T

# Overhauser Effect in Insulating Solids

- OE reported in solid samples of BDPA in polystyrene
- Spectral density ascribed to fluctuations of radical
- No diffusion, dominated by Fermi contact, works at high field

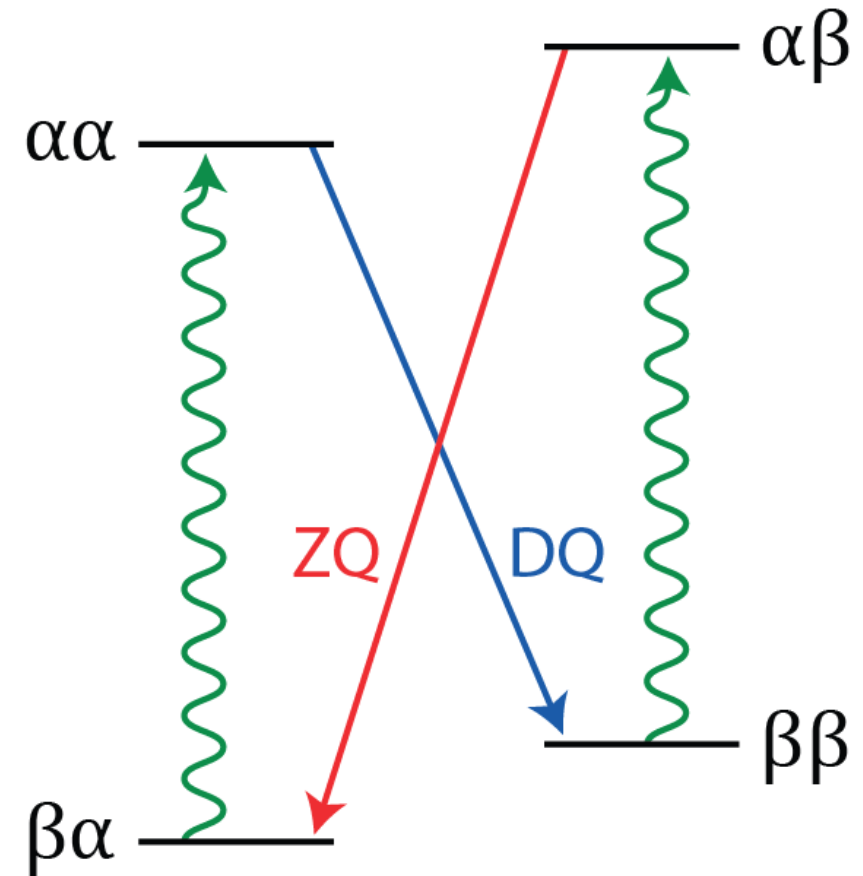


Can et al., *J. Chem. Phys.*, 2014  
 Pylaeva et al., *J. Phys. Chem. Lett.*, 2017



# Overhauser Effect Summary

- Electron resonance saturated
- Cross relaxation with nucleus generates hyperpolarisation
- Sign of enhancement depends on **ZQ** vs **DQ** rate
- Mainly used in liquids
- Only works at low field (<1 T) unless dominated by scalar coupling



Questions?

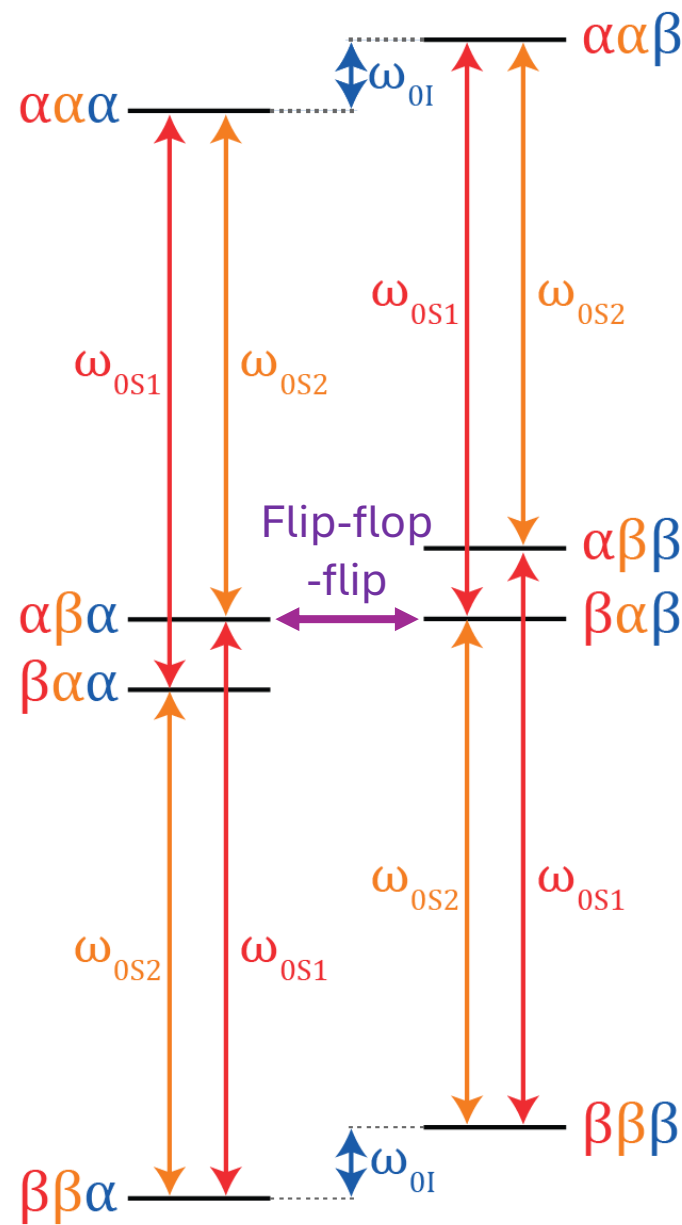
# Cross effect



Alexander Kessenikh

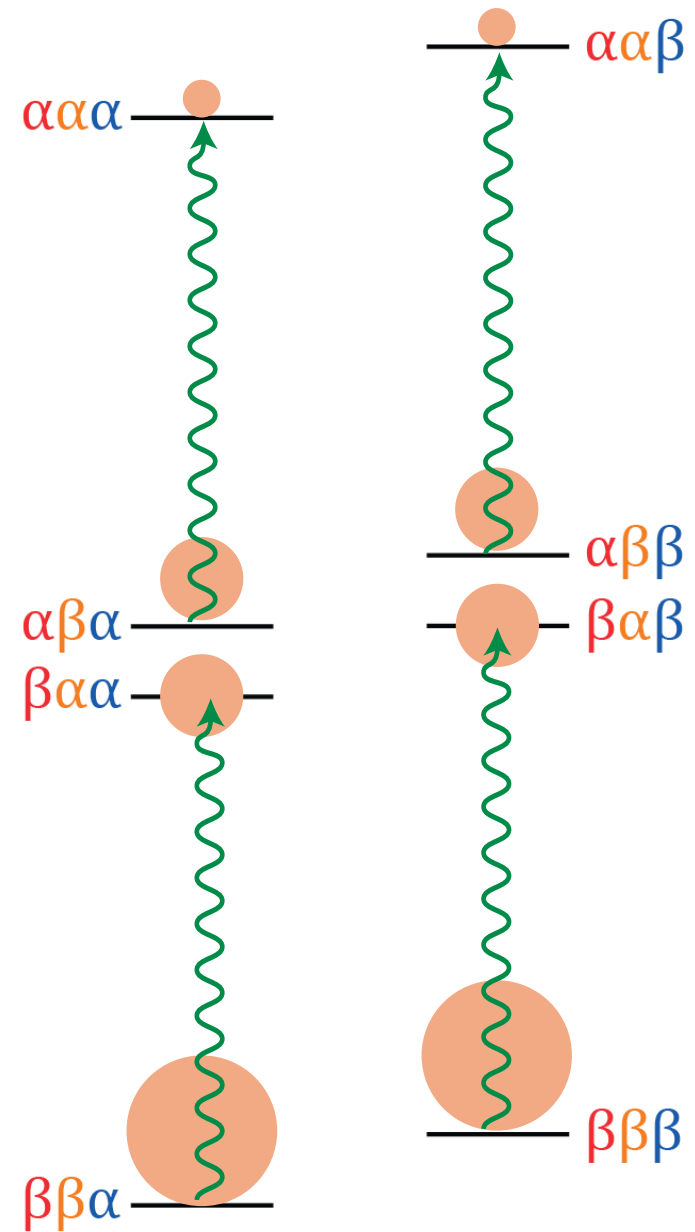
# Cross Effect

- Cross effect is a three-spin process
- Consider two coupled electrons, at least one of which is coupled to a nucleus
- Matching condition:  $\omega_{0S1} - \omega_{0S2} = \omega_{0I}$
- Flip-flop-flip transitions conserve energy
- (Weakly allowed due to state mixing. Requires anisotropic e-e coupling and e-n coupling. Like SE, but more complicated maths!)



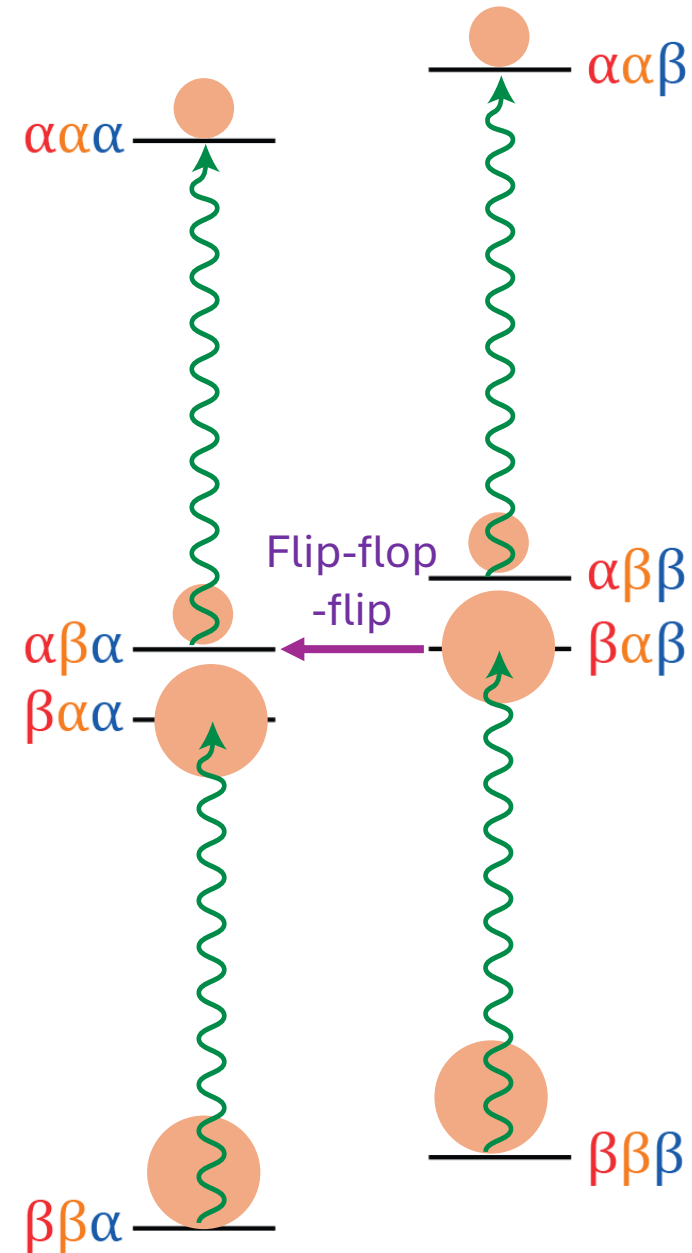
# Cross Effect

- Saturate one electron with microwaves (shown for  $S_2$ )



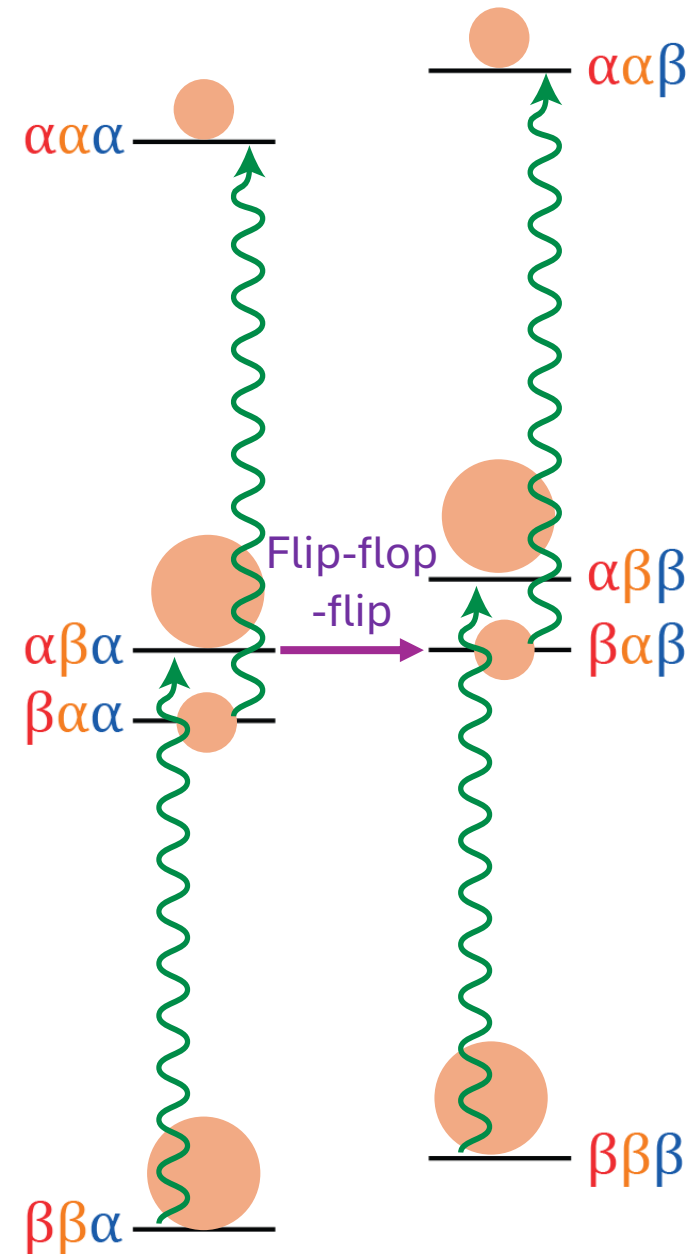
# Cross Effect

- Saturate one electron with microwaves (shown for  $S_2$ )
- The population of the degenerate levels are no longer equal, so the flip-flop-flip rates are unequal, generating nuclear hyperpolarisation
- Define  $\omega_{0S1} > \omega_{0S2}$
- $\omega_{\mu w} = \omega_{0S2}$ ,  $|\beta\alpha\beta\rangle \rightarrow |\alpha\beta\alpha\rangle$   
Positive enhancement

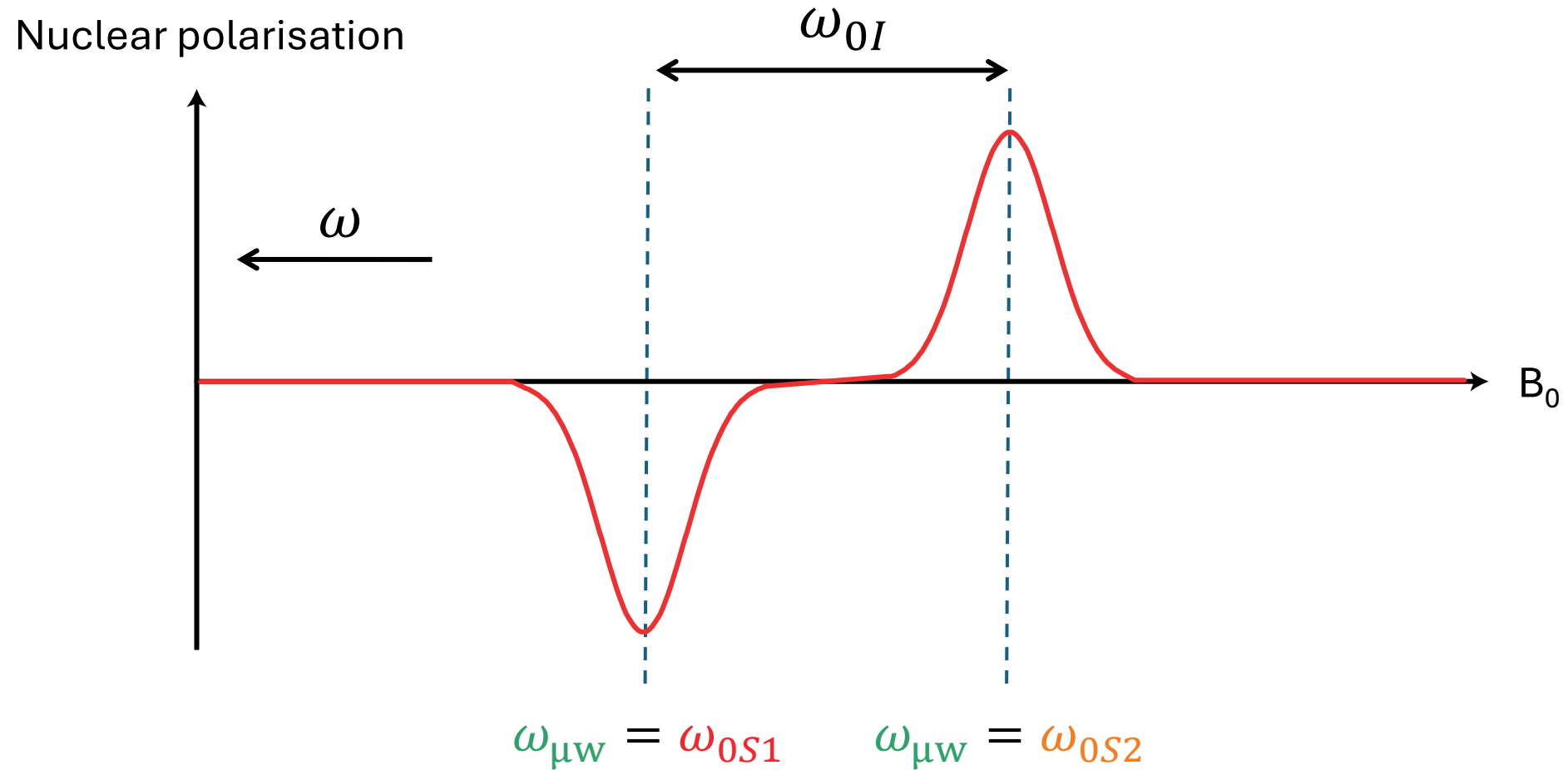


# Cross Effect

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- $\omega_{\mu w} = \omega_{0S2}$ ,  $|\beta\alpha\beta\rangle \rightarrow |\alpha\beta\alpha\rangle$   
Positive enhancement
- $\omega_{\mu w} = \omega_{0S1}$ ,  $|\alpha\beta\alpha\rangle \rightarrow |\beta\alpha\beta\rangle$   
Negative enhancement



# Cross Effect Field Profile

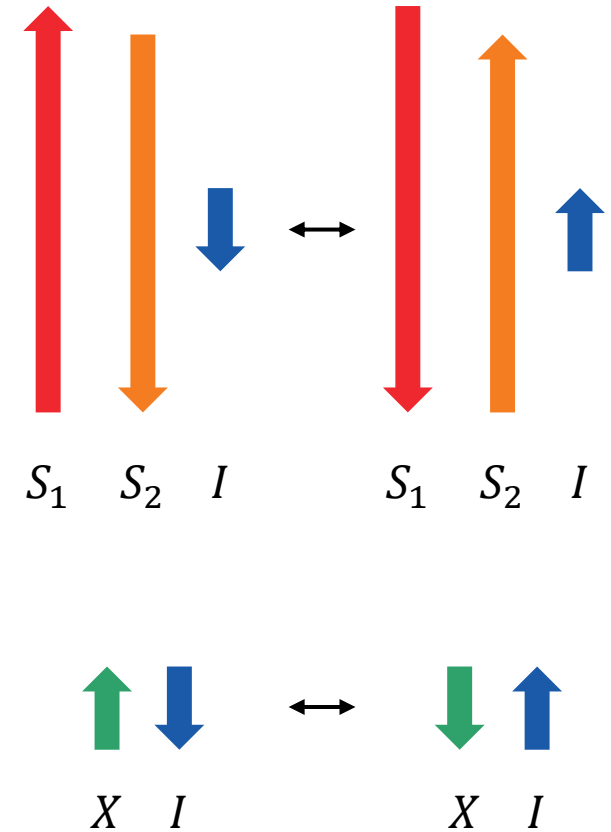


Matching condition:  $\omega_{0S1} - \omega_{0S2} = \omega_{0I}$

So lobes are separated by  $\omega_{0I}$

# Cross effect with a fictitious spin

- Can consider a fictitious spin  $X = S_1 - S_2$
- $E_X = E_{S_1} - E_{S_2} = E_I$  (cross-effect condition)
- Cross effect = flip-flops between  $X$  and  $I$
- Polarisation  $P_X = P_{S_1} - P_{S_2}$
- Thermal equilibrium,  $P_X$  given by Boltzmann.  
 $E_X = E_I$ , so  $P_X = P_I$
- If  $S_2$  is saturated,  $P_X = P_{S_1}$ , i.e. large polarisation
- Cross effect transfers polarisation from  $X$  to  $I$

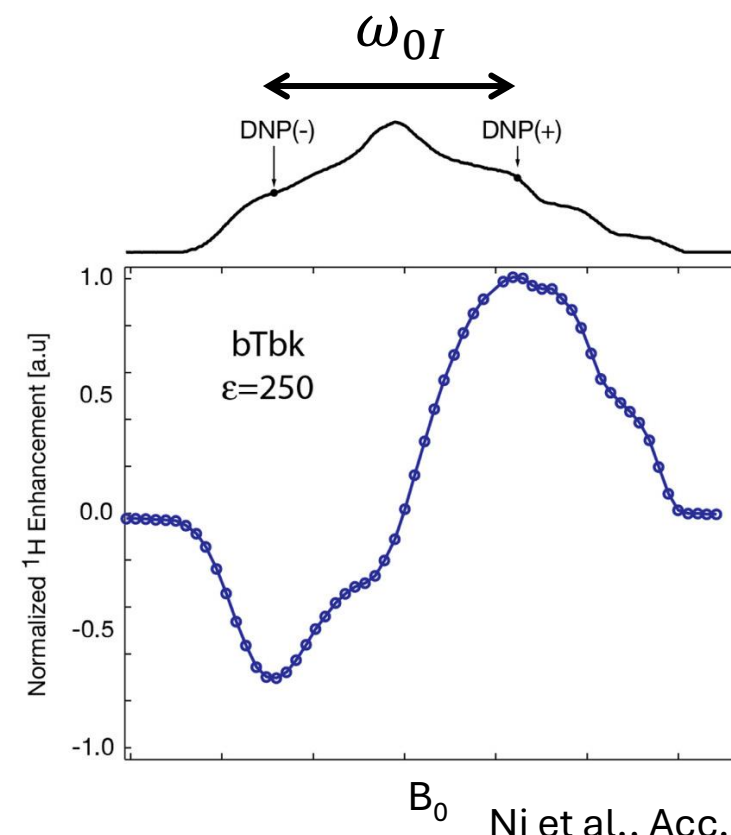
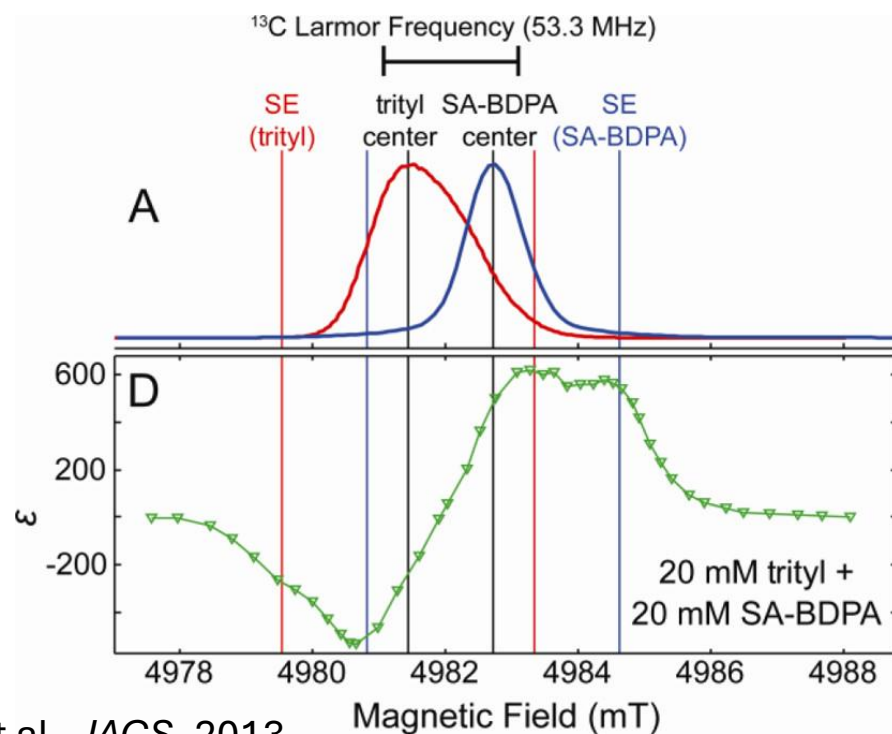




# How to achieve the matching condition?

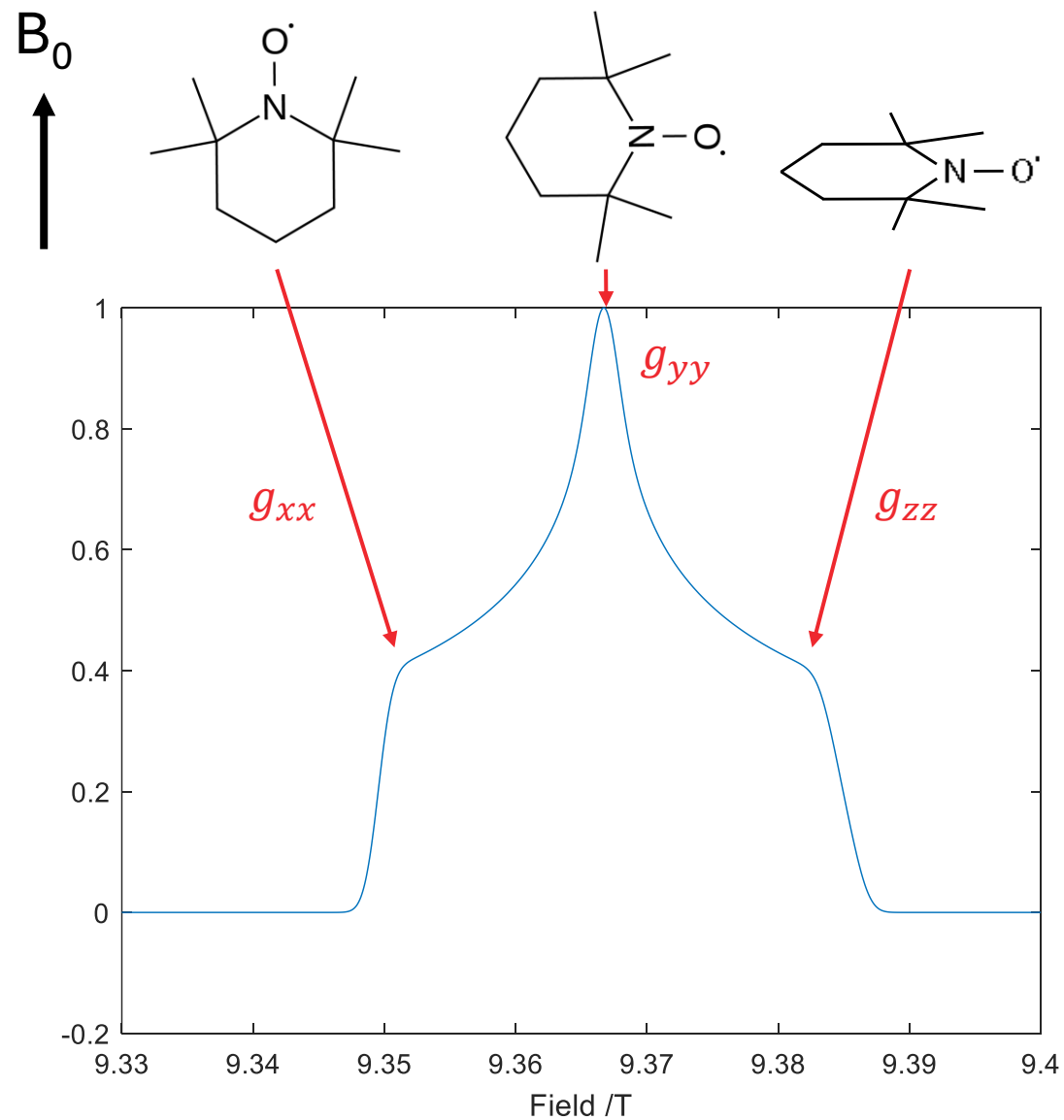
$$\omega_{0S1} - \omega_{0S2} = \omega_{0I}$$

- Two narrow line radicals that happen to match for a certain nucleus
- Difficult to achieve in practice!
- A broad-line radical where the anisotropy is greater than the nuclear Larmor frequency



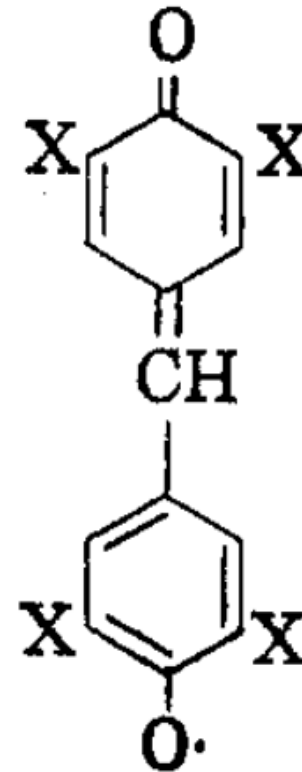
# g Anisotropy

- For broadline radicals, electron  $g$  value depends on orientation
- Analogous to CSA in NMR
- Radicals with different orientations in the sample have different EPR frequencies



# Cross effect with monoradicals

- Cross effect was originally observed for high concentrations (5%) of monoradicals with g-anisotropy dissolved in a polystyrene glass
- Only works when two radicals with the right orientations so that  $\omega_{0S1} - \omega_{0S2} = \omega_{0I}$  happen to be near each other
- This is unlikely, reducing the enhancement and requiring high concentrations!

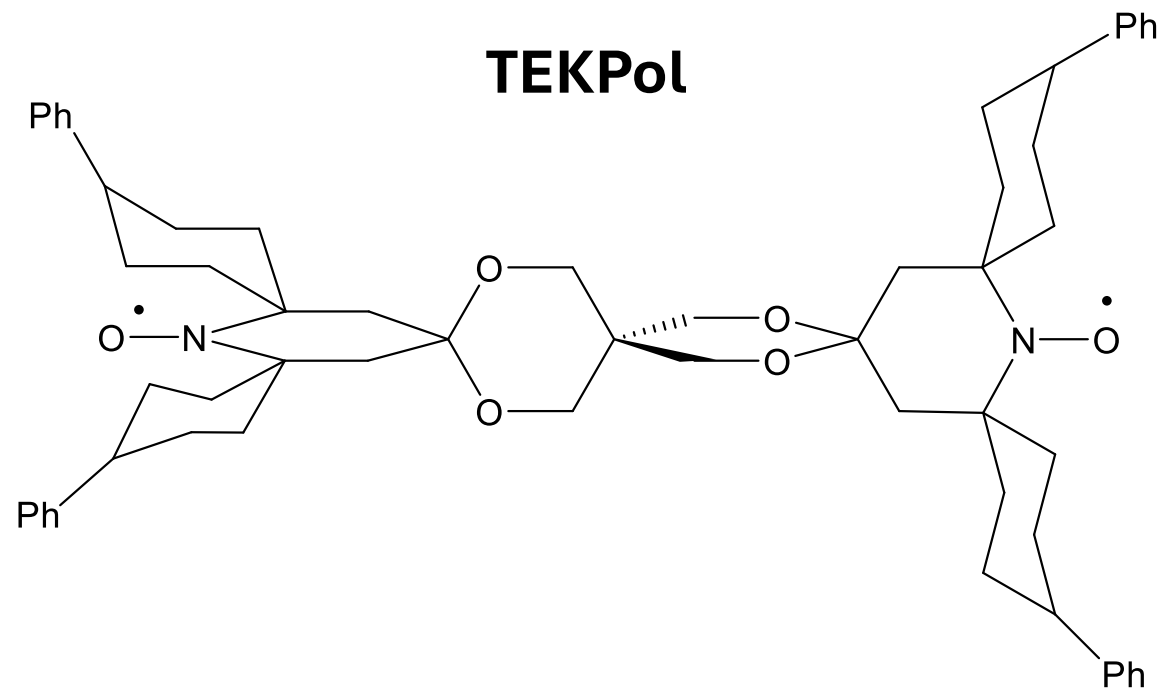


Ley's radical

**X** = *tert*-butyl

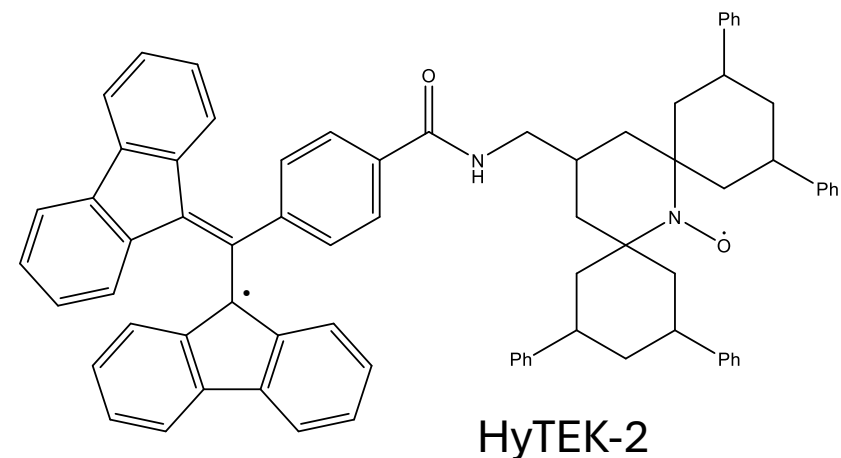
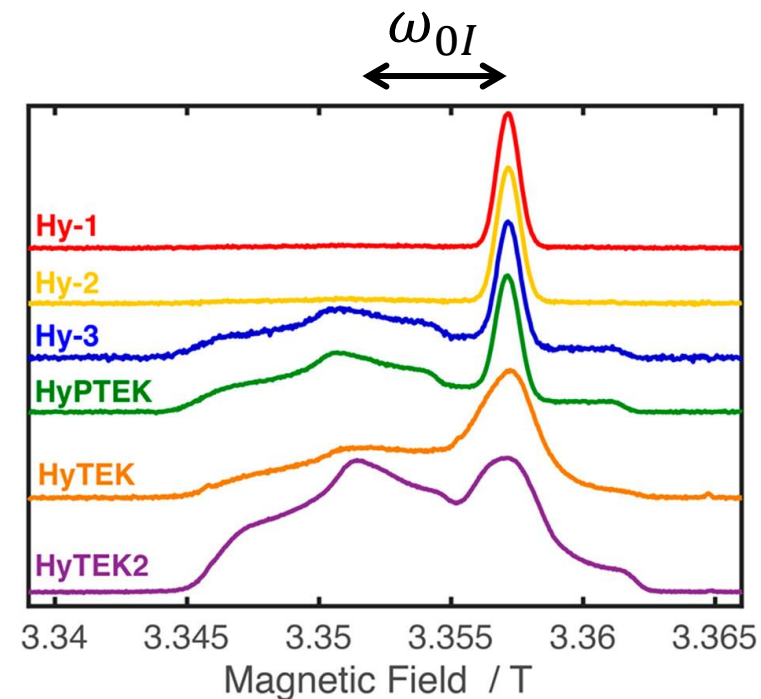
# Biradicals

- Tethered biradicals ensure that there are two electrons close together, even at low concentrations
- Designed so that the g-tensors are  $\sim$ orthogonal so the electrons have different frequencies
- Optimised e-e distance to give large dipolar coupling, without too fast relaxation
- Bulky groups give long  $T_{1e}$  and  $T_{2e}$  to increase electron saturation
- Enhancement by factor  $\epsilon_H \approx 200$



# Hybrid biradicals

- Bi-nitroxides were optimised at 9.4 T (400 MHz)
- EPR linewidth  $\propto B_0$  when dominated by  $g$  anisotropy
- At higher field, becomes harder to saturate, reducing enhancement ( $\varepsilon \approx 20$  at 900 MHz)
- Hybrid biradicals have a narrow line radical tethered to a wideline radical
- Narrow line can be easily saturated
- Narrow – wide =  $\omega_{0I}$
- $\varepsilon \approx 200$  at 900 MHz

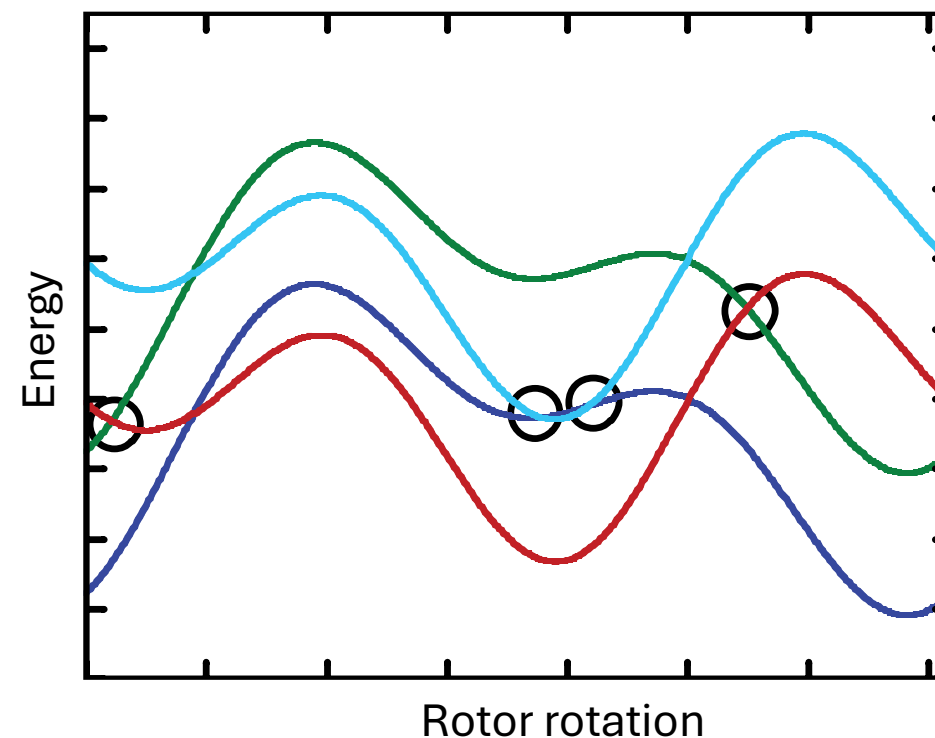
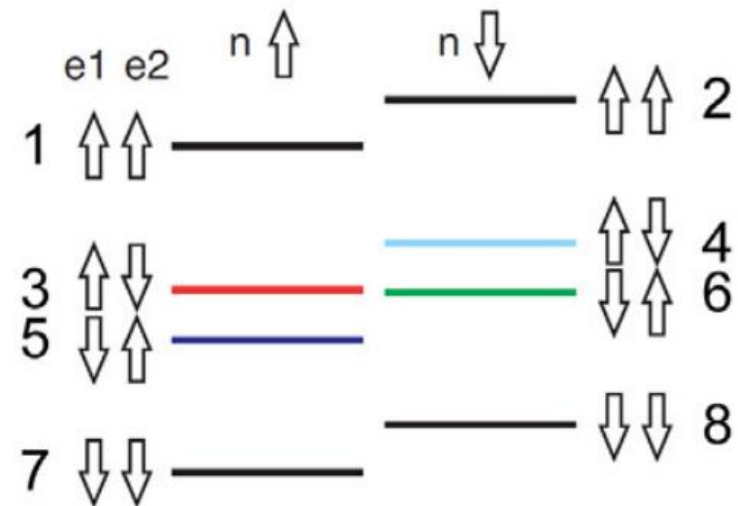


# MAS DNP

What about the MAS?

# Cross Effect under MAS

- Electron frequencies are orientation dependent
- Under MAS, they become time dependent
- At certain orientations, the levels have the same energy
- Called a level crossing



# Types of Level Crossing



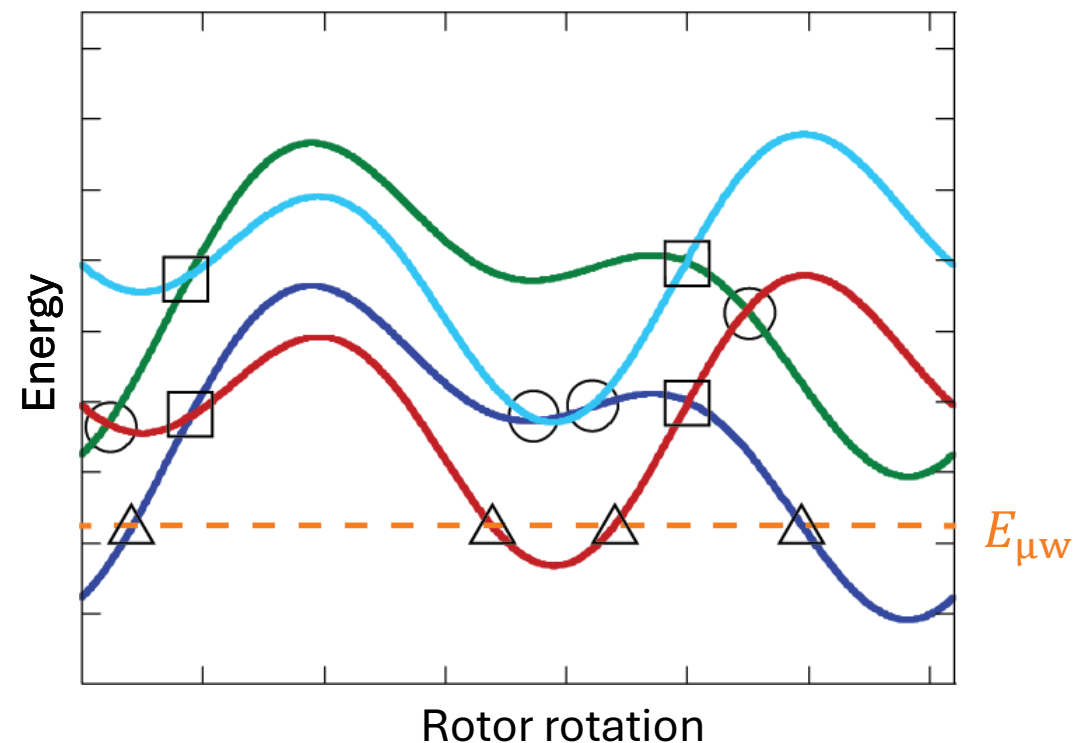
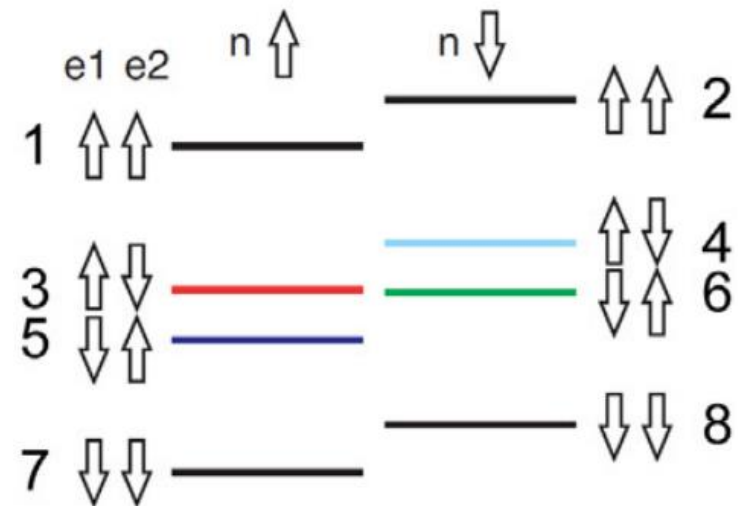
- Cross effect flip-flop-flips (circles):  $|\beta\alpha\beta\rangle \leftrightarrow |\alpha\beta\alpha\rangle$   
Generate nuclear polarisation



- Electron-electron flip-flop (squares):  $|\beta\alpha\rangle \leftrightarrow |\alpha\beta\rangle$   
Exchange electron saturation



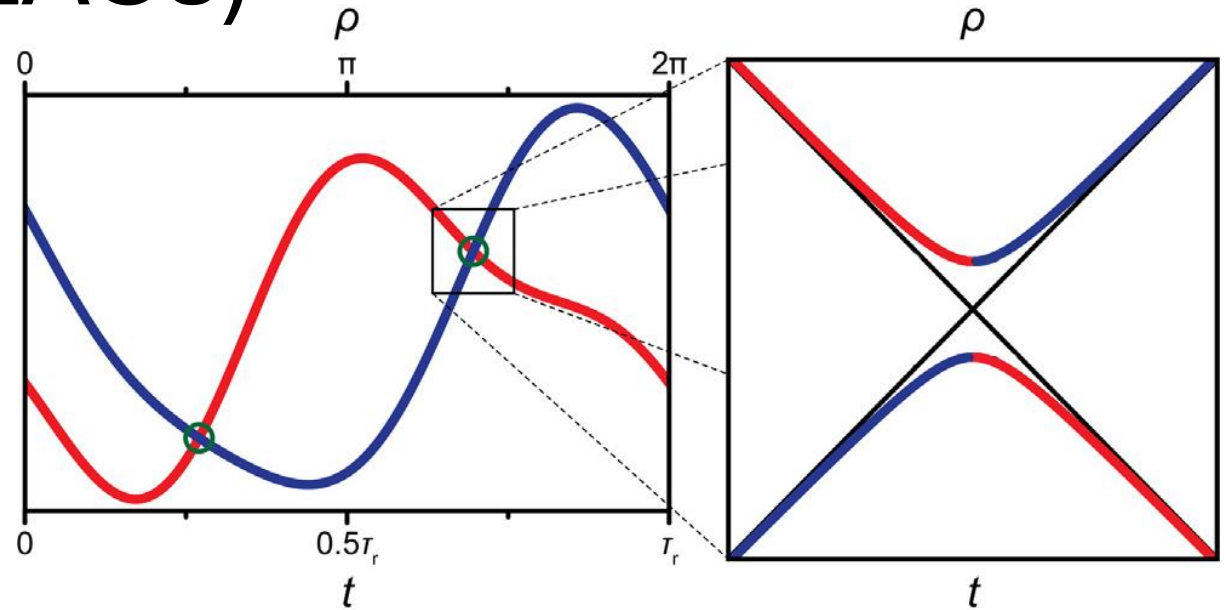
- Microwave-driven electron spin flips (triangles)  
 $|\alpha\rangle \leftrightarrow |\beta\rangle$  and  $|\alpha\rangle \leftrightarrow |\beta\rangle$   
Saturate the electron





# Level anti crossings (LACs)

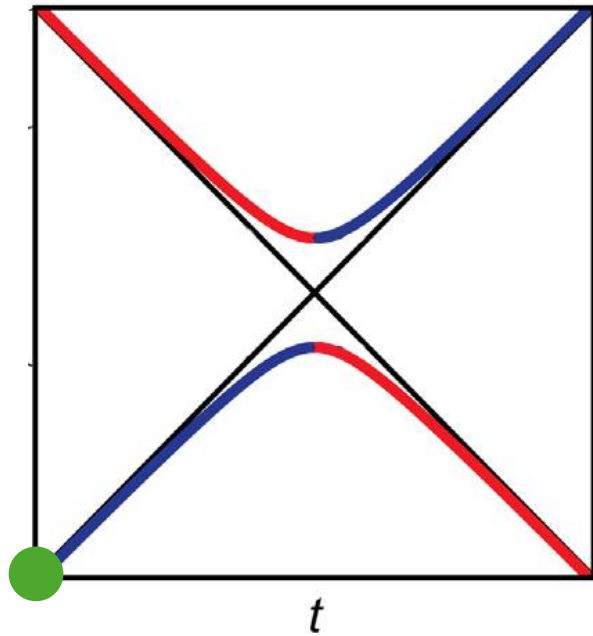
- Off-diagonal elements cause state mixing when the energy difference is small enough



- $\hat{H} = \begin{pmatrix} E_1 & 0 \\ 0 & E_2 \end{pmatrix}$  has eigenstates with energies  $E_1$  and  $E_2$
- $\hat{H} = \begin{pmatrix} E_1 & W \\ W & E_2 \end{pmatrix}$  has energies  $E = \frac{1}{2}(E_1 + E_2) \pm \frac{1}{2}\sqrt{(E_1 - E_2)^2 + 4W^2}$
- When  $W$  and  $(E_1 - E_2)$  are comparable, in vicinity of crossing, the levels repel
- Known as a level anti-crossing or avoided level crossing

# What happens at a LAC?

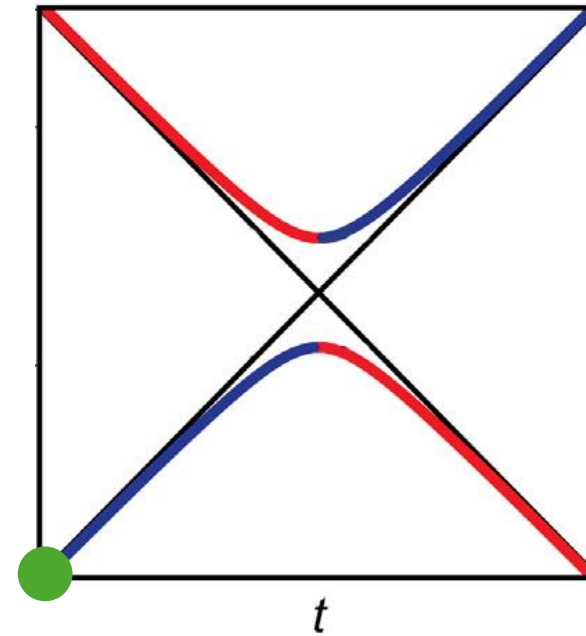
## Fast Passage



Stays in the same unperturbed state

Non-adiabatic

## Slow Passage



Follows the eigenstates

Adiabatic

# How fast or slow?

- Landau-Zener equation:
- Probability of changing state (adiabatic passage),

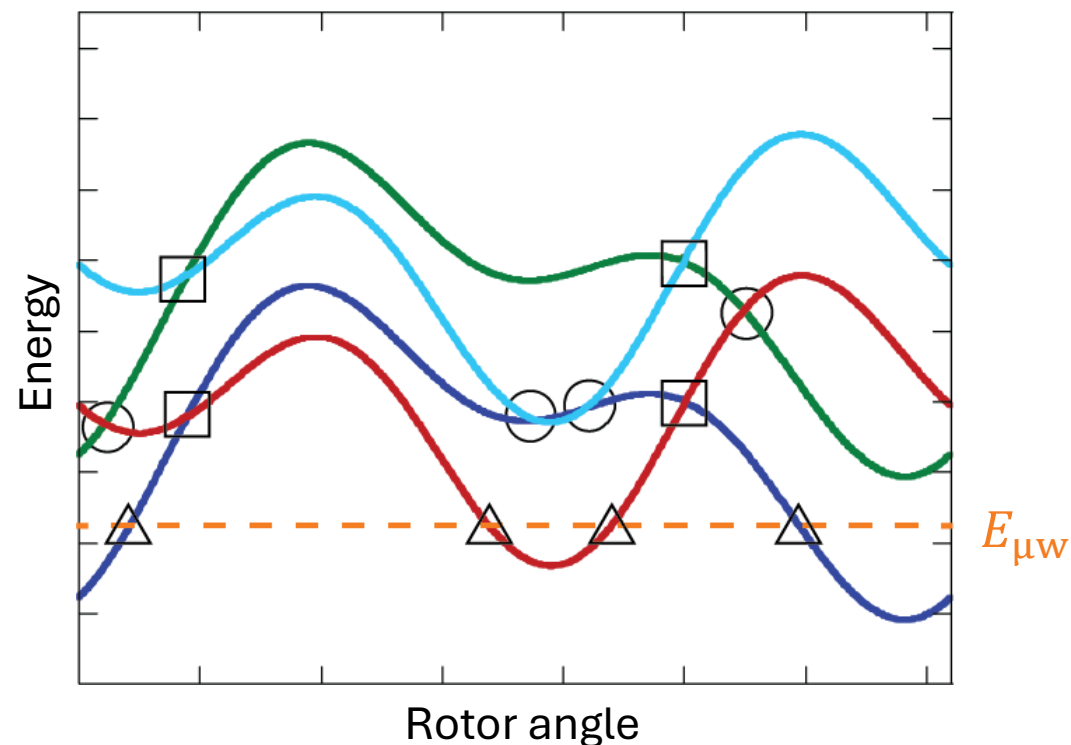
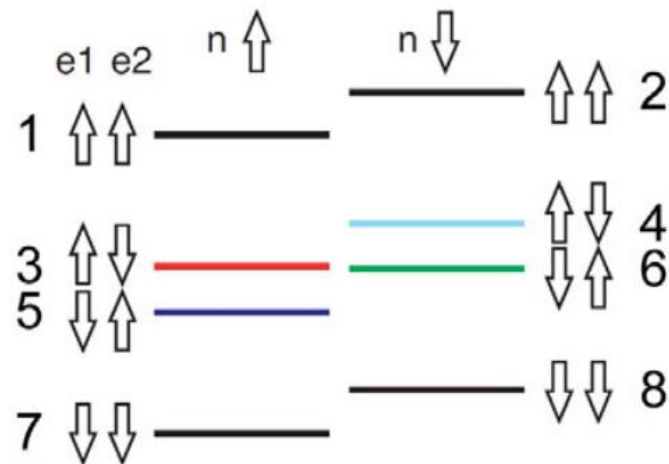
$$P = 1 - \exp\left(-\frac{2\pi W^2}{d\Delta E/dt}\right)$$

- High probability for large coupling ( $W$ ) and slow transit (small  $\frac{d\Delta E}{dt}$ )

# Adiabaticity of crossings

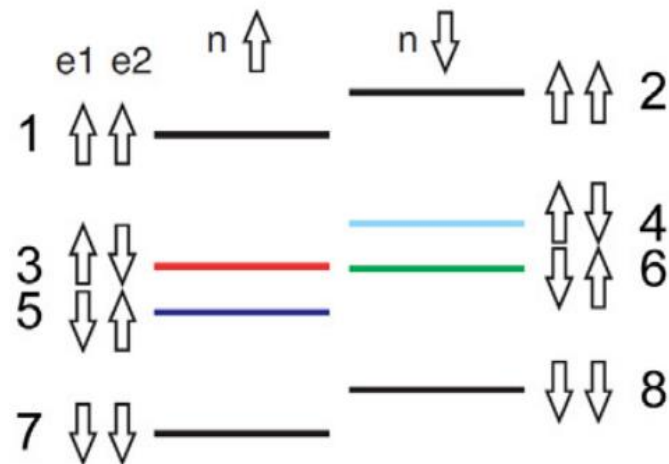
- △
- Microwave-driven spin flips:  $P \sim 50\%$
  - Allowed transitions, large  $W$ .  
The electron can be saturated quite easily over a few rotor periods

- 
- Electron-electron flip-flops:  
 $P \approx 0.999999$
  - Strong e-e coupling, so electron saturation almost always transfers
  - The saturated electron is always the lower (higher) energy electron, so the enhancement is always positive (negative) and doesn't cancel out.

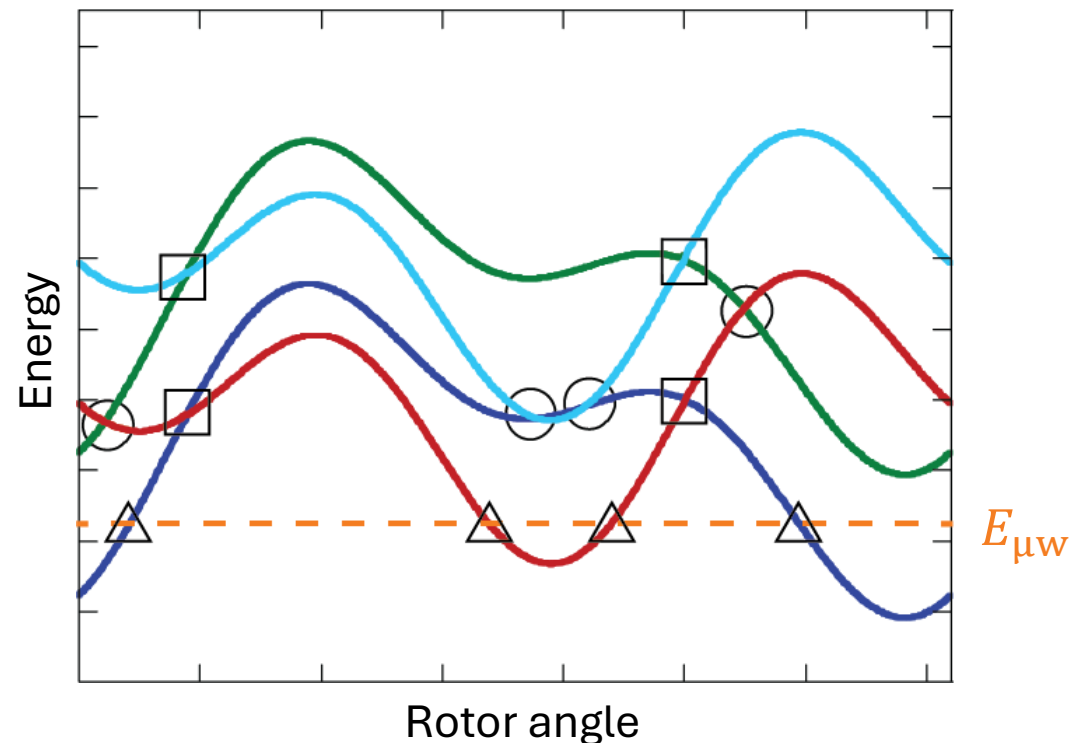


# Adiabaticity of crossings

- Cross effect flip-flop-flips:  $P \sim 0.1\%$
- Probability of cross effect transition is low
- Nuclear  $T_1 \sim 1 - 10 \text{ s} = 10^3 - 10^4$  rotor periods
- Over many events, hyperpolarisation builds up



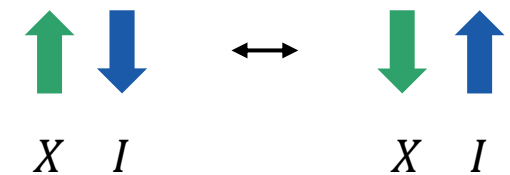
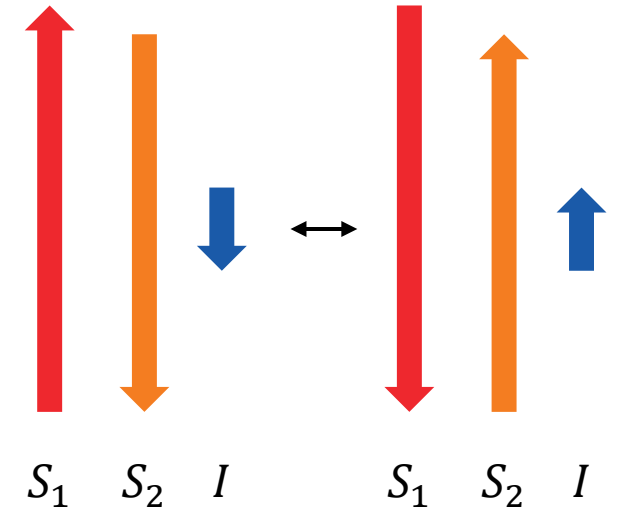
- Magic-angle spinning separates the electron-microwave and cross-effect events in time
- Conditions do not need to be simultaneously satisfied
- Many more orientations contribute to DNP, improving enhancements



# Depolarisation

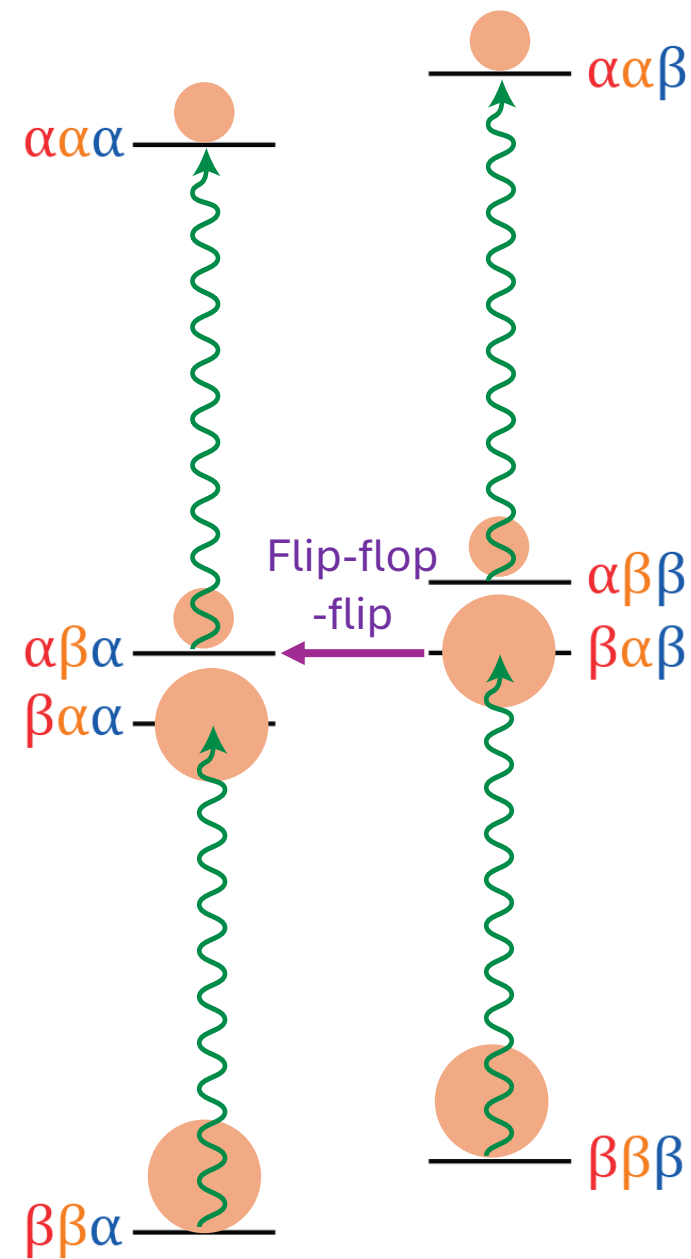
- In the absence of microwaves, the cross effect events still occur
- Electron-electron flip-flops also occur, acting to equalise the electron polarisations, reducing the difference polarisation  $P_X = P_{S1} - P_{S2}$
- $P_X < P_I$ , so cross effect *reduces* the nuclear polarisation
- This is called depolarisation
- Reduction in NMR signal under MAS, without microwaves
- Signal enhancement is overestimated vs thermal  

$$\varepsilon = I_{\text{ON}}/I_{\text{OFF}}$$



# Cross Effect Summary

- Two coupled electrons and a coupled nuclear spin
- One of the electrons is saturated by microwaves
- Cross-effect flip-flop-flips transfer electron difference polarisation to nucleus
- Typically biradicals with g-anisotropy are used to satisfy  $\omega_{0S1} - \omega_{0S2} = \omega_{0I}$
- Under MAS, saturation and cross-effect events happen at different points of the rotor period, making CE more efficient



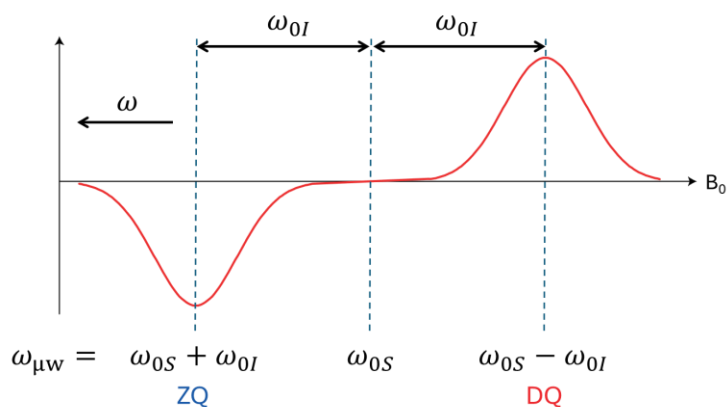
Questions?

# Summary



## Solid Effect

Drive forbidden e-n  
ZQ/DQ transitions



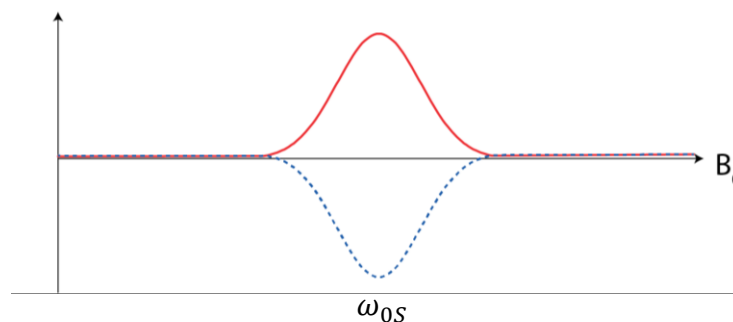
Narrow EPR line

Solid state

High  $\mu w$  power  
(weakly allowed)

## Overhauser Effect

Saturate SQ electron,  
e-n cross relaxation



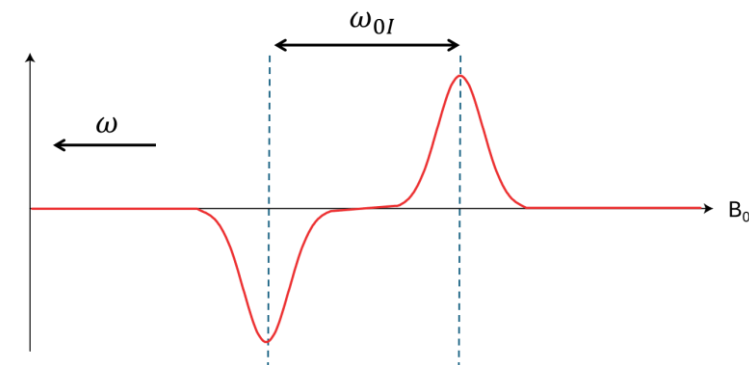
Narrow EPR line

Mainly liquid state

Lower  $\mu w$  power

## Cross Effect

Saturate one electron,  
e-e-n flip-flop-flip transitions



Broad inhomogeneous EPR  
(typically biradicals)

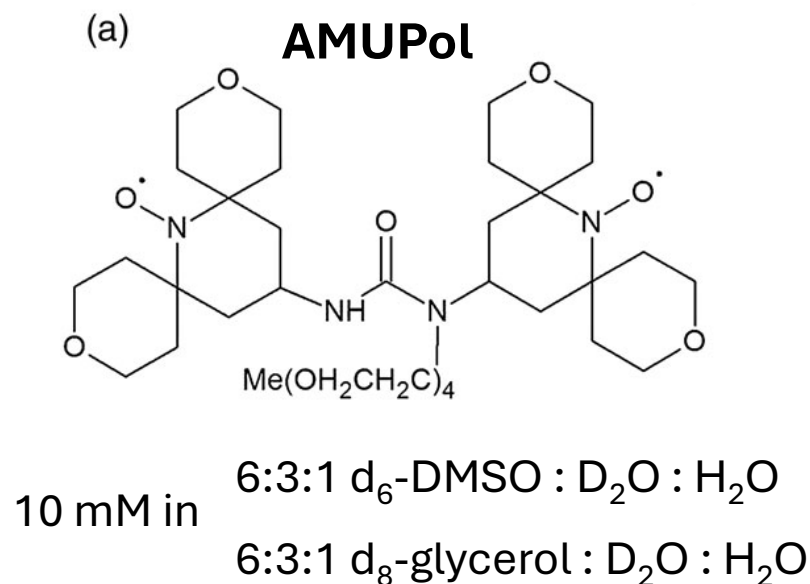
Solid state

Medium  $\mu w$  power  
(Broader EPR)

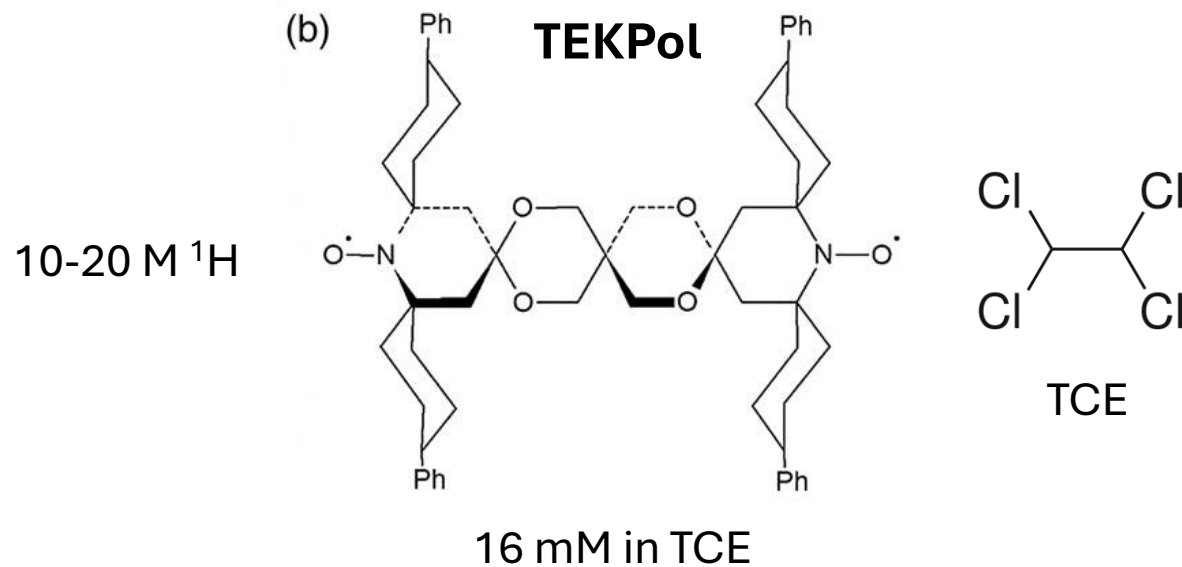
# Running DNP experiments

# DNP of Frozen Solutions

- Polarising agent (e.g. biradical) is dissolved in a glass-forming solvent (along with a target molecule)
- Flash frozen to form a glass with well dispersed radical
- Partially deuterated solvent so hyperpolarisation not diluted too much
- Radical concentration optimised to give enough polarisation sources, without strong radical-radical interactions



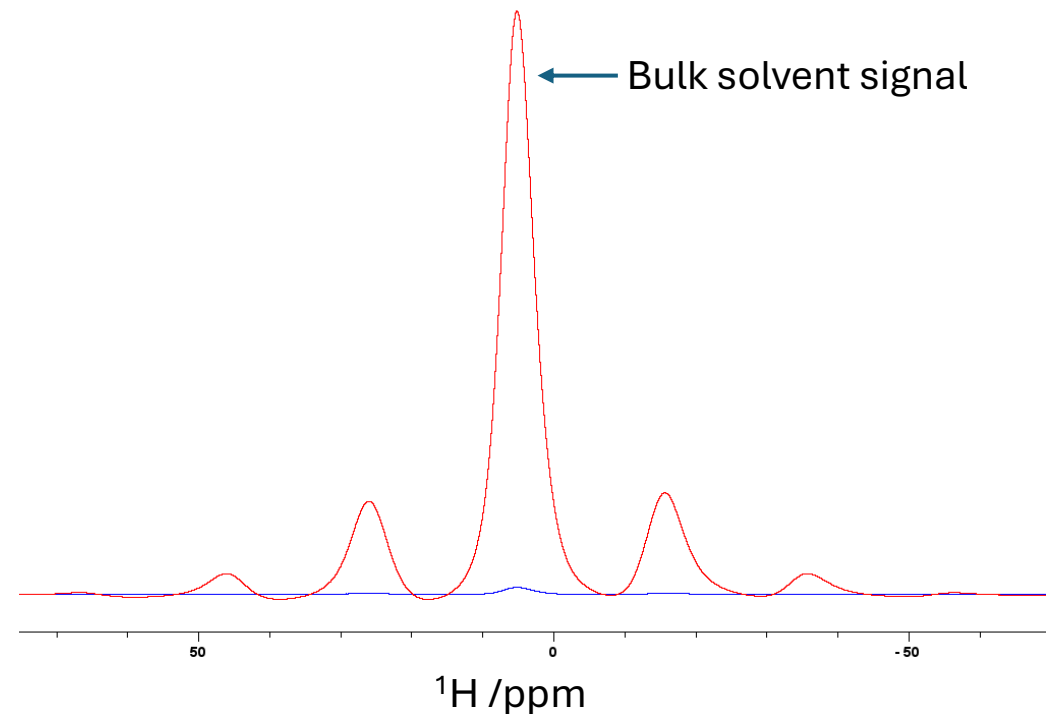
Sauvée et al., *Angew. Chem.*, 2013



Zagdoun et al., *JACS*, 2013

# DNP of Frozen Solutions

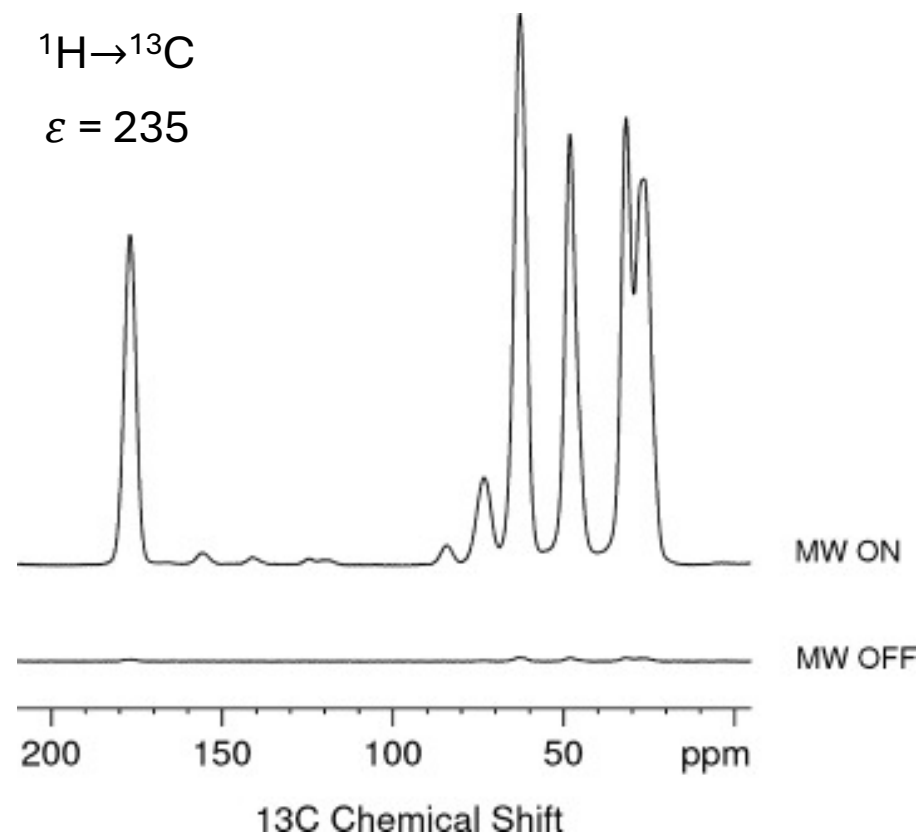
- Probe pre-cooled to 100 K
- Warm sample is (quickly) inserted to flash freeze
- For organic solvents (e.g. TCE), multiple insert/eject cycles to degas oxygen (paramagnetic relaxation sink)
- Turn on microwaves!
- $^1\text{H}$ - $^1\text{H}$  spin diffusion relays hyperpolarisation away from radicals to enhance the bulk of the solvent (and dissolved target)



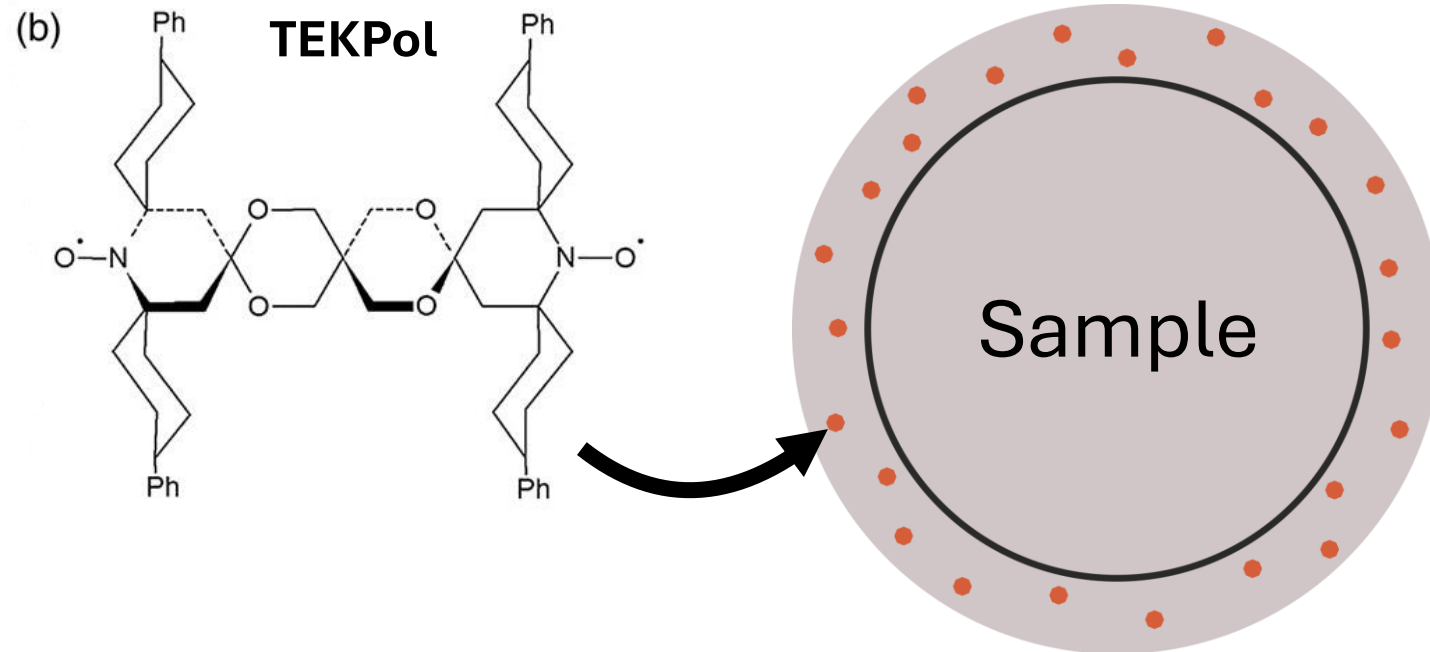
# “Indirect DNP”

- After  $^1\text{H}$ - $^1\text{H}$  spin diffusion relays polarisation throughout the sample, cross polarisation transfers to the nucleus of interest
- Benefit from faster  $^1\text{H}$  spin diffusion

0.25 M Proline  
10 mM AMUPol  
6:3:1  $\text{d}_8$ -glycerol: $\text{D}_2\text{O}$ : $\text{H}_2\text{O}$

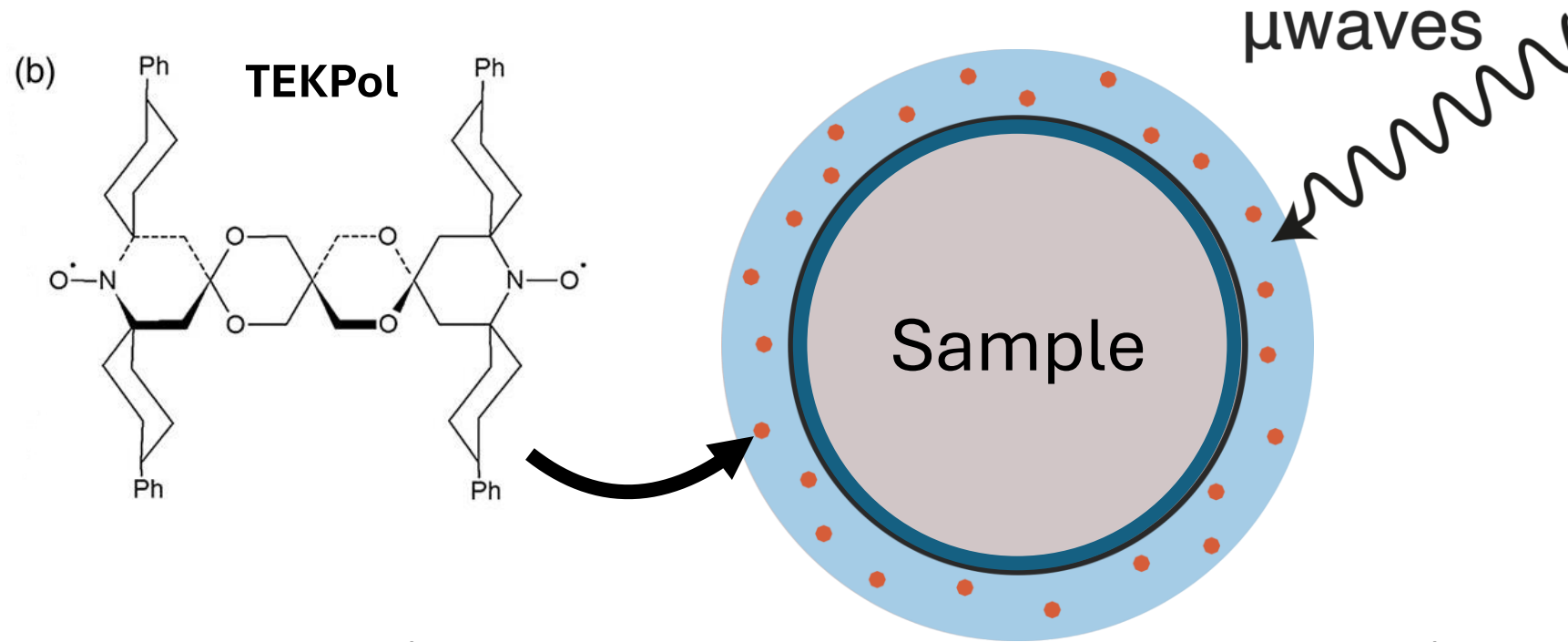


# Impregnation DNP



- Powdered sample is wetted with solution of polarising agents (just enough to coat the surfaces!)
- Can fill the pores of porous materials to access internal surfaces

# Impregnation DNP



## Indirect DNP

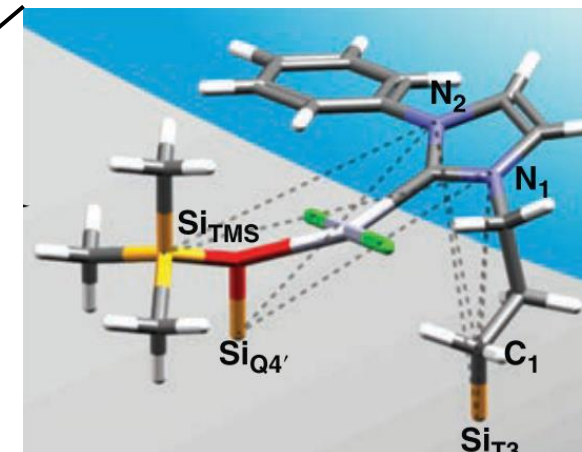
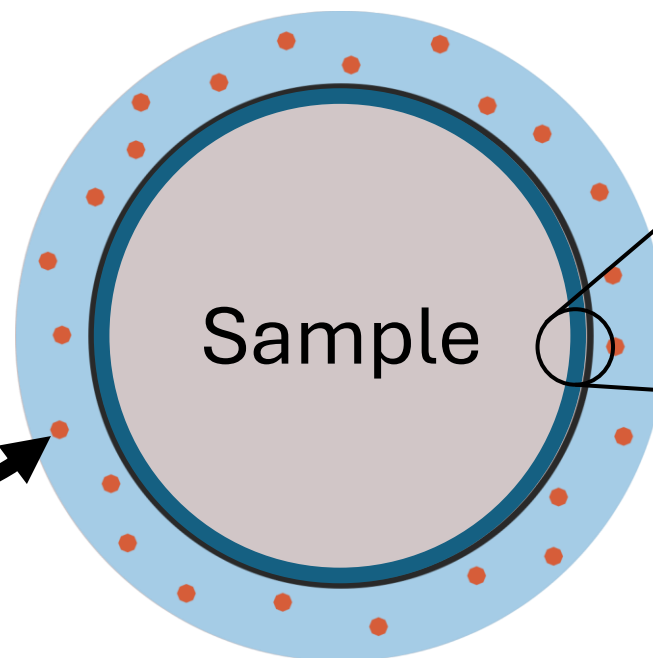
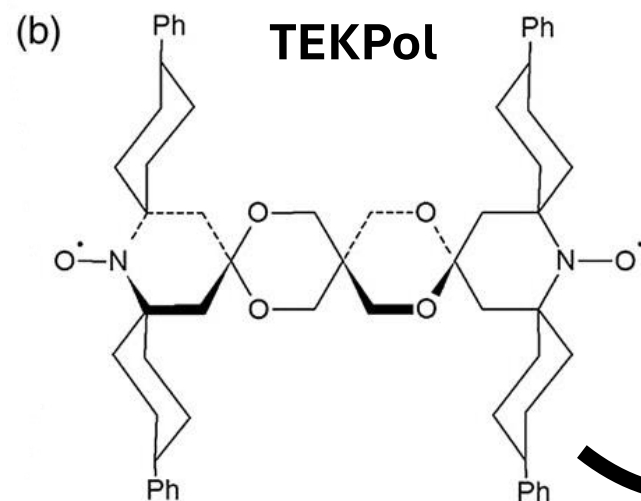
- Transfer from  $^1\text{H}$  to nucleus of interest by CP
- Surface-selective if no  $^1\text{H}$  in bulk

## Direct DNP

- Nucleus directly polarised by DNP
- Surface-selective due to slow X spin diffusion

# DNP Surface-Enhanced NMR (SENS)

Rossini et al., *Acc. Chem. Res.*, 2013



## Indirect DNP

- Transfer from  $^1\text{H}$  to nucleus of interest by CP
- Surface-selective if no  $^1\text{H}$  in bulk

## Direct DNP

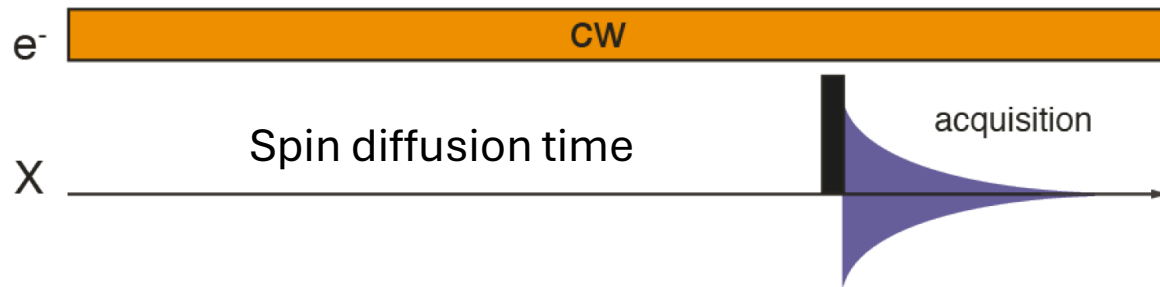
- Nucleus directly polarised by DNP
- Surface-selective due to slow X spin diffusion



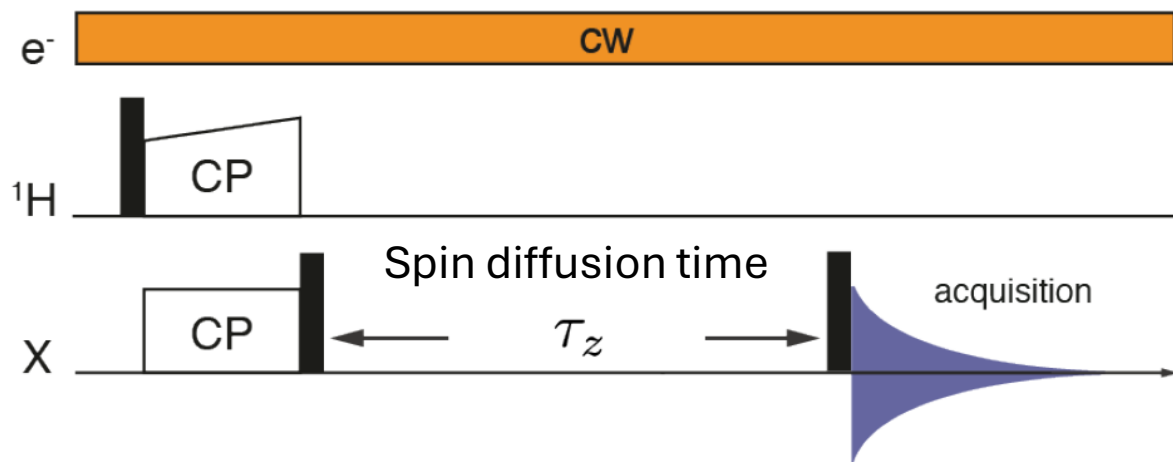


# Relayed DNP by X spin diffusion

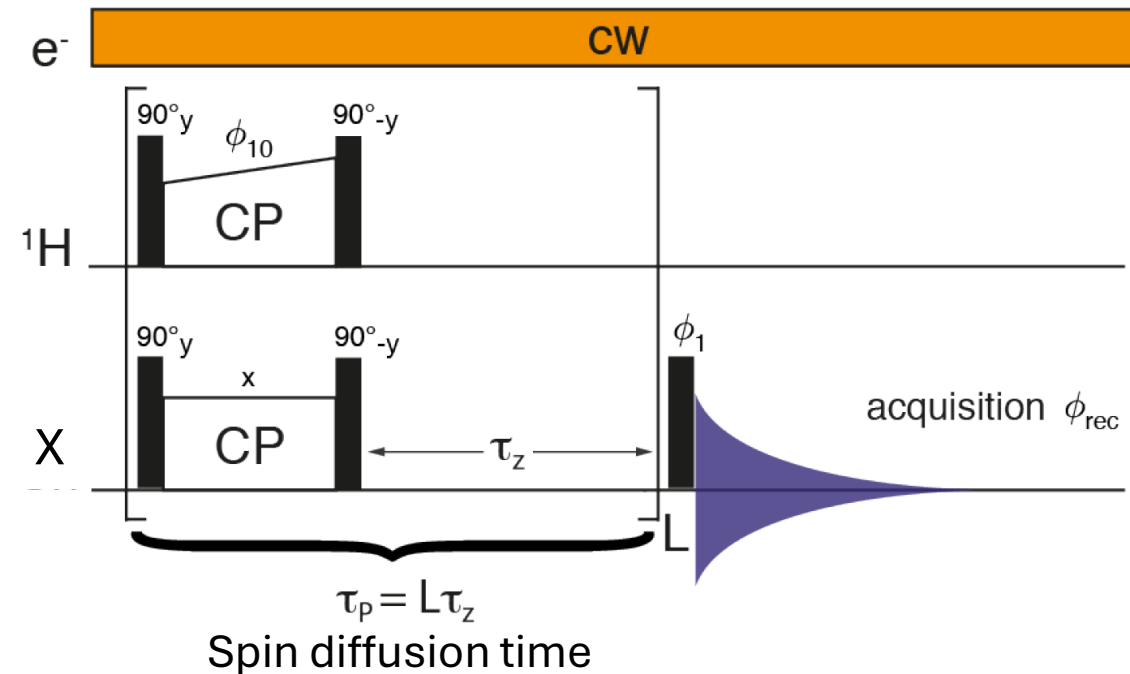
## Direct DNP



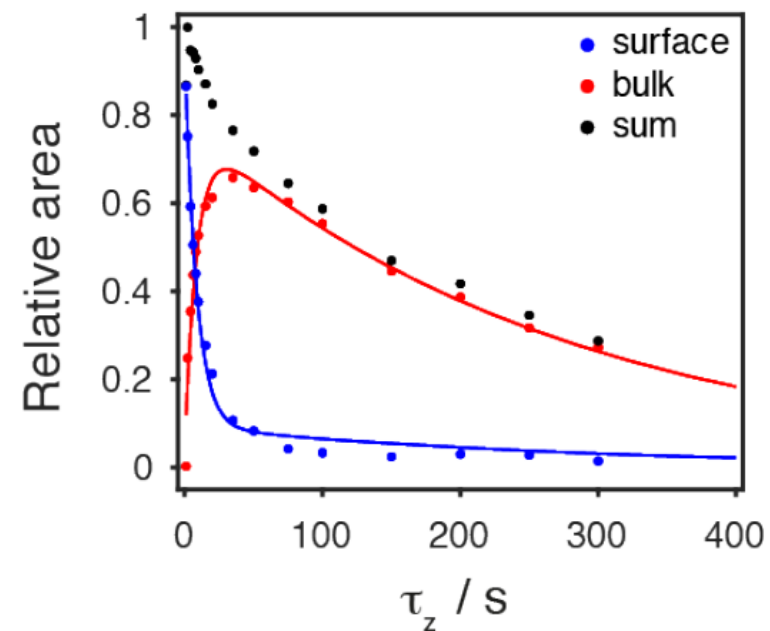
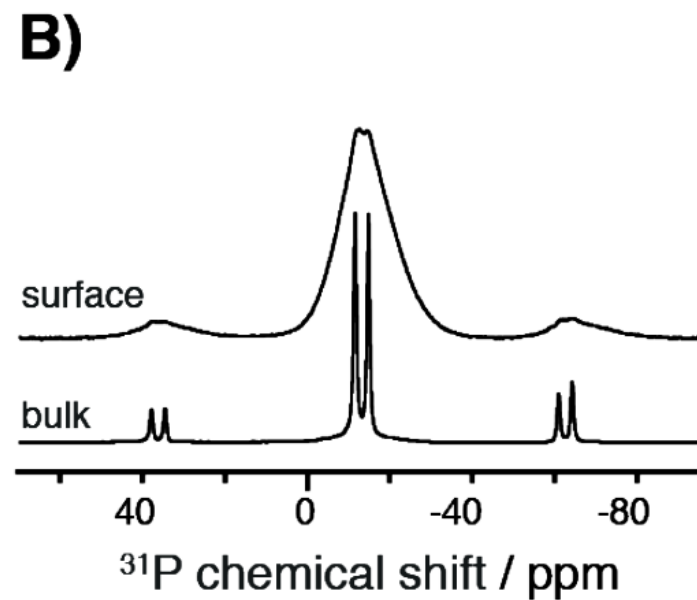
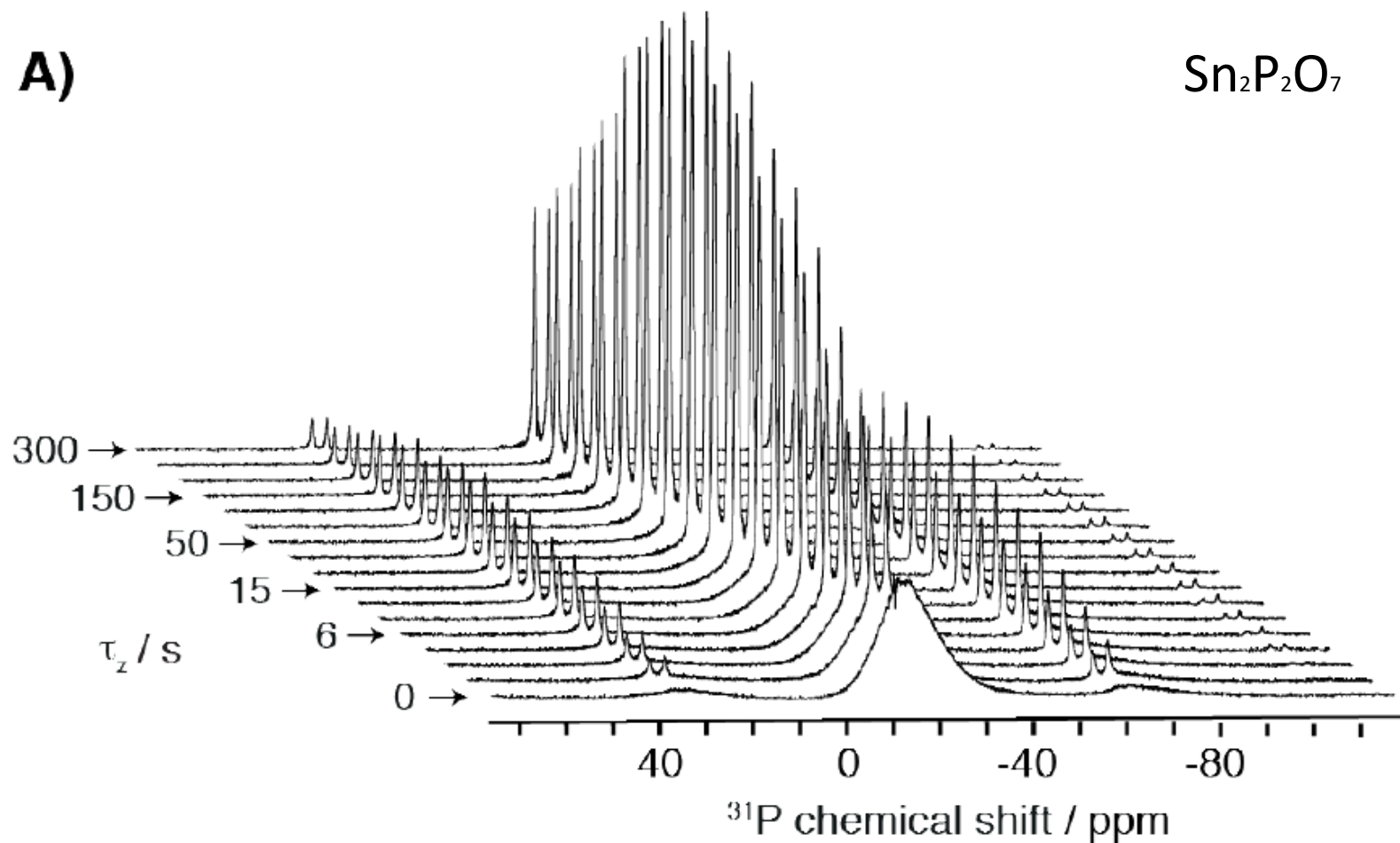
## Indirect DNP + Z-filter



## Indirect DNP + Multi-CP



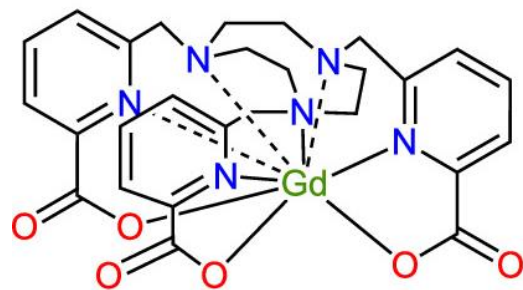
# Relayed DNP



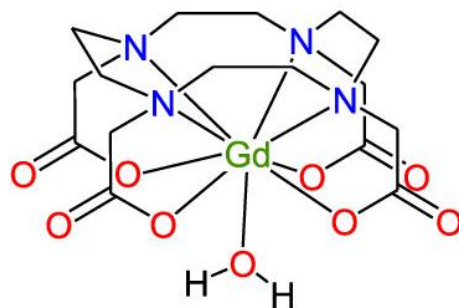
# Metal-ion DNP

- Most paramagnetic metals relax too quickly for efficient DNP
- **Except** high-spin ions with no orbital angular momentum
- $\text{Mn}^{2+}$  ( $S = 5/2$ ),  $\text{Gd}^{3+}$  ( $S = 7/2$ ), octahedral  $\text{Cr}^{3+}$  ( $S = 3/2$ )
- Primarily solid effect
- $S > 1/2$ , subject to zero-field splitting (ZFS)
- Analogous to nuclear quadrupolar coupling. High-symmetry environment needed for narrow lines and efficient DNP

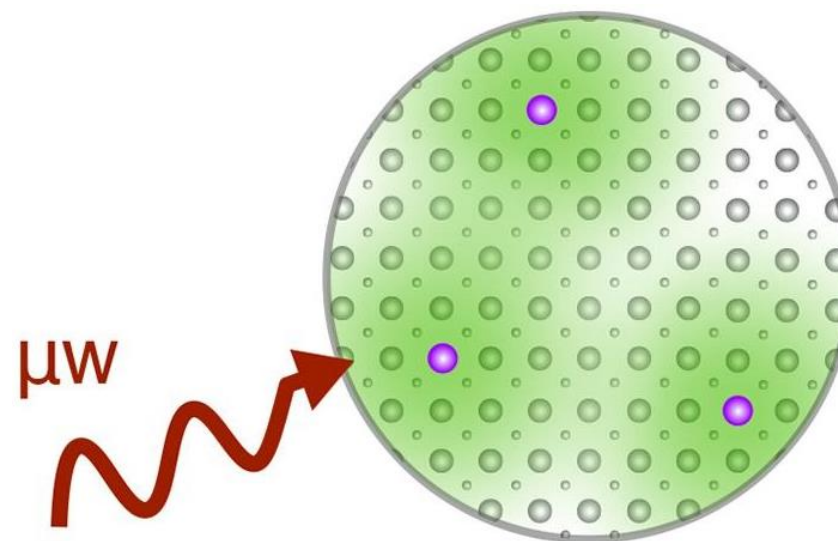
# Metal-ion DNP



[Gd(tpacn)]



[Gd(dota)(H<sub>2</sub>O)]<sup>-</sup>



## “Exogenous” DNP

- High-symmetry Gd complexes for frozen-solution / impregnation DNP
- More stable to reduction, e.g. in cell

Stevanato et al., *JACS*, 2019

## “Endogenous” DNP

- Metal-ion doped into material
- Inherent bulk sensitivity
- Symmetric sites can give large  $\epsilon$

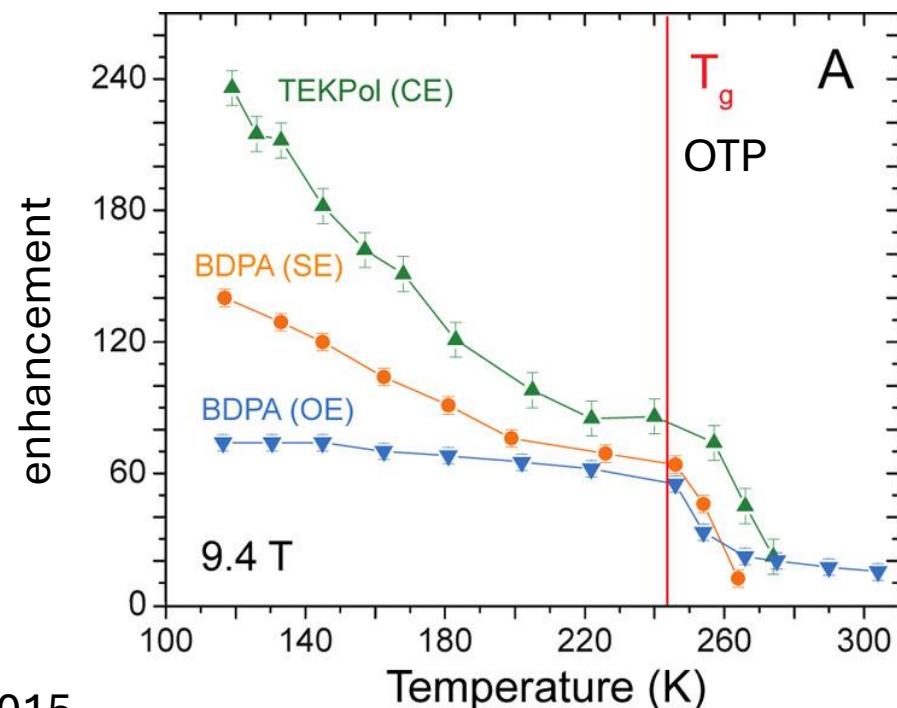
Jardon-Alvarez and Leskes, *Prog. Nucl. Magn. Reson. Spec.* 2023

# Summary of DNP Flavours

- Impregnation / exogenous DNP
  - Indirect DNP,  $^1\text{H} \rightarrow \text{X}$ 
    - $^1\text{H}$  in sample,  $^1\text{H} \rightarrow \text{X}$  CP : **bulk**
    - No  $^1\text{H}$  in sample
      - $^1\text{H} \rightarrow \text{X}$  CP : **surface**
      - $^1\text{H} \rightarrow \text{X}$  multi-CP : **bulk**
  - Direct DNP of X nuclei
    - Short recycle delay : **surface**
    - Long recycle delay (assuming  $T_1$  is long enough!) : **bulk**
- Endogenous DNP : **bulk**

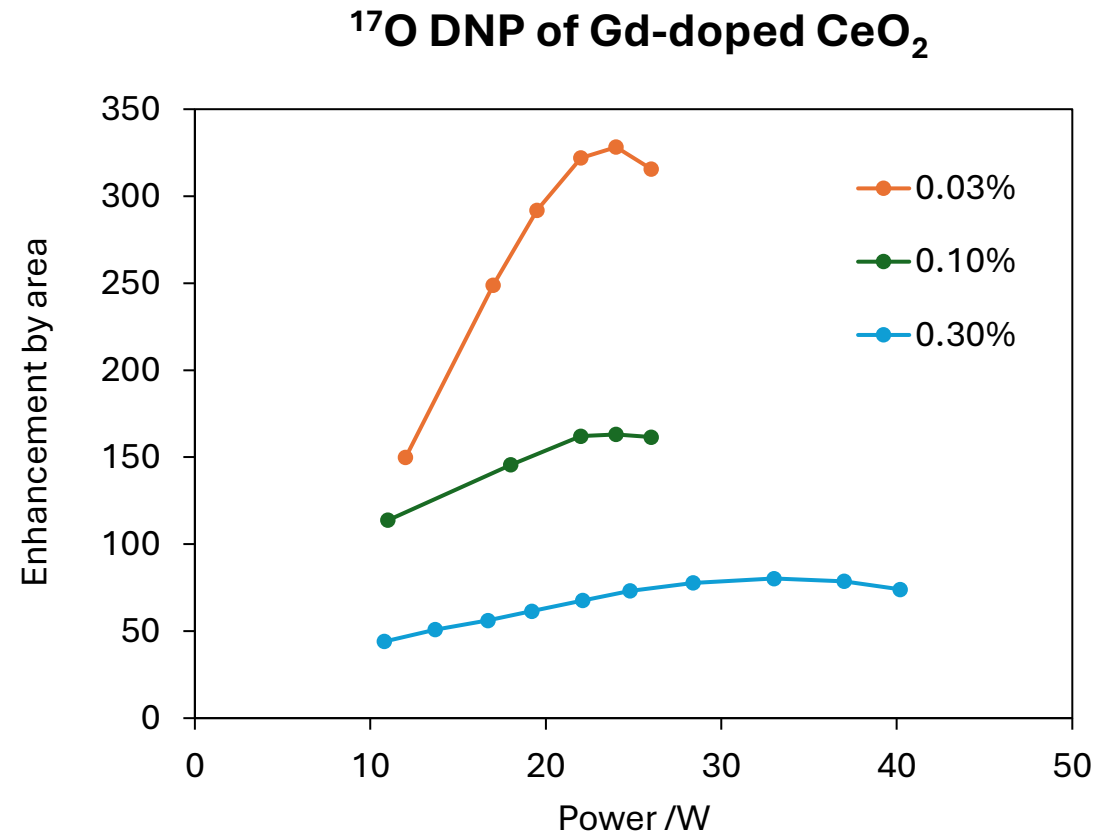
# Temperature

- Commercial MAS DNP systems use LN2: ~100 K
- Helium spinning has also been demonstrated: 30 – 40 K
- Low T slows down the electron relaxation, so it's easier to saturate the transitions
- T dependence also determined by rigidity of glass (and  $T_g$ )
- Overhauser effect often run at room temp: e.g., liquids, or Li metal ( $T_{1e}$  temp independent)



# Microwave Power

- Balance greater microwave field with higher sample temp to maximise saturation





# With thanks to...

- Warwick NMR group
- Moreno Lelli
- Lyndon Emsley & LRM group
- Federico De Biasi
- Pinelopi Moutzouri
- Pierrick Berruyer

## Progress in Nuclear Magnetic Resonance Spectroscopy

Dynamic nuclear polarization for sensitivity enhancement in modern solid-state NMR

Aany Sofia Lilly Thankamony<sup>1</sup>, Johannes J. Wittmann<sup>1</sup>, Monu Kaushik, Björn Corzilius\*

# Appendix: Sensitivity in NMR

# Sensitivity in NMR

$T_2^*$ : inverse of the linewidth

$M_m$ : nuclear magnetisation  
(molar)

$t_{\text{exp}}$ : experimental time

$c$ : concentration

$$\text{SNR} \approx M_m c \eta T_2^* \sqrt{\frac{t_{\text{exp}} \omega_0 V_C \mu_0 Q \Delta f}{T_1 4 F k_B T_C}}$$

$T_1$  relaxation constant

$\omega_0$ : Larmor frequency

$T_C$ : temperature of the coil

$\eta$ : volume filling-factor in the coil

$V_C$ : volume of coil

$Q$  = Q factor of coil.  $F$ : noise factor.  $\Delta f$  = receiver bandwidth

# How to increase sensitivity?

- Increase concentration
- Increase  $T_2^*$  (e.g. MAS, decoupling)
- Go to higher field ( $\text{SNR} \propto B_0^{3/2}$ )
- Make your coil and sample bigger
- Use a cryoprobe
- Reduce  $T_1$  (e.g. PRE)
- Run for longer!
- **Increase Magnetisation**

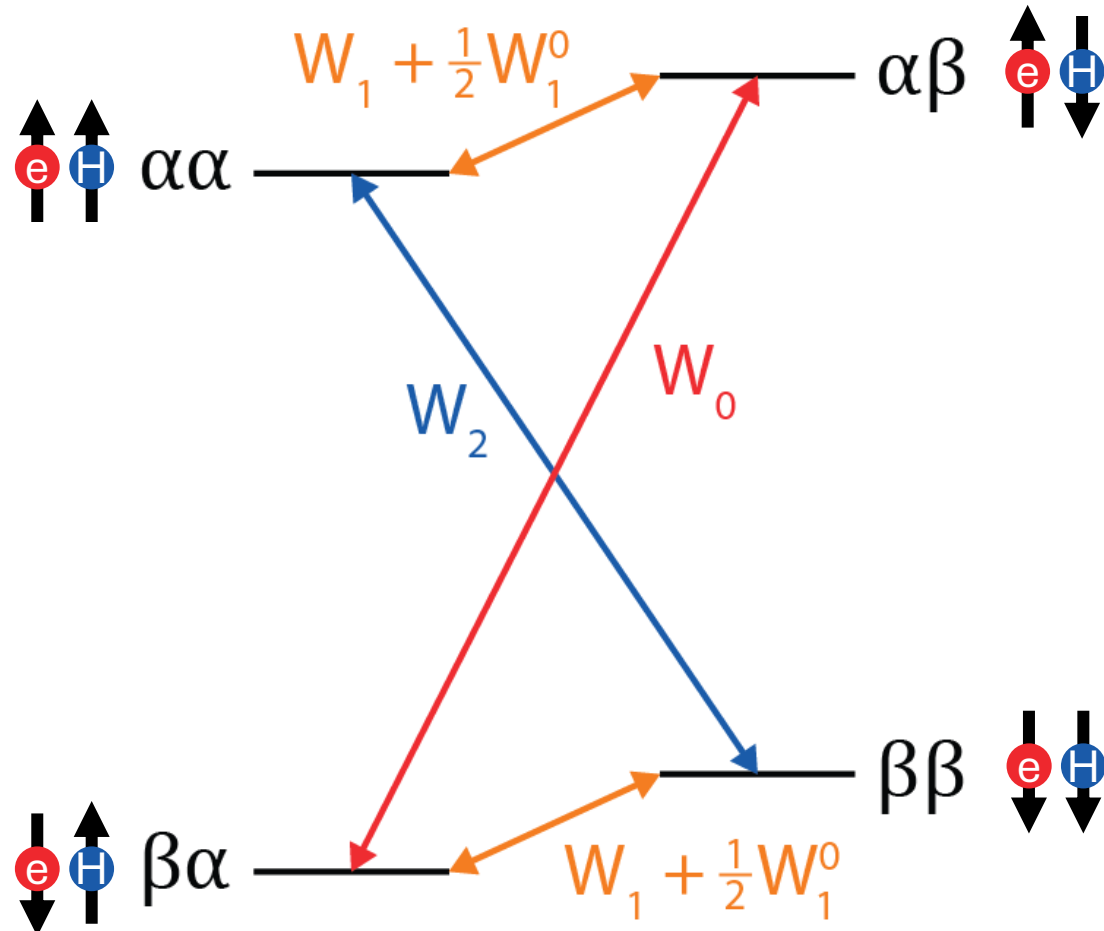
$$\text{SNR} \approx M_m c \eta T_2^* \sqrt{\frac{t_{\text{exp}} \omega_0 V_C \mu_0 Q \Delta f}{T_1 4F k_B T_C}}$$



# Appendix:

## Overhauser effect relaxation rates

# Overhauser Effect: Rate Equations



- $W_i = 1^{\text{st}}$  order relaxation rate coefficient for each transition
- $W_1 =$  nuclear relaxation induced by e-n coupling
- $W_1^0 =$  nuclear relaxation by any other source =  $1/T_1^{\text{pure}}$

$$\frac{d\langle I_z \rangle}{dt} = -(W_0 + 2W_1 + W_2 + W_1^0)(\langle I_z \rangle - I_0) - (W_2 - W_0)(\langle S_z \rangle - S_0)$$

# Overhauser Effect: Rate Equations

$$\frac{d\langle I_z \rangle}{dt} = -(W_0 + 2W_1 + W_2 + W_1^0)(\langle I_z \rangle - I_0) - (W_2 - W_0)(\langle S_z \rangle - S_0) = 0$$

$$(\langle I_z \rangle - I_0) = \frac{W_2 - W_0}{W_0 + 2W_1 + W_2 + W_1^0} (S_0 - \langle S_z \rangle)$$

$$\frac{\langle I_z \rangle - I_0}{I_0} = \frac{W_2 - W_0}{W_0 + 2W_1 + W_2 + W_1^0} \frac{S_0 - \langle S_z \rangle}{S_0} \frac{S_0}{I_0}$$

Enhancement:  $\varepsilon = \frac{\langle I_z \rangle}{I_0} = 1 + \frac{W_2 - W_0}{W_0 + 2W_1 + W_2 + W_1^0} \frac{W_0 + 2W_1 + W_2}{W_0 + 2W_1 + W_2 + W_1^0} \frac{S_0 - \langle S_z \rangle}{S_0} \frac{\gamma_S}{\gamma_I}$

# Overhauser Effect: Rate Equations

$$\varepsilon = \frac{\langle I_z \rangle}{I_0} = 1 + \frac{W_2 - W_0}{W_0 + 2W_1 + W_2} \frac{W_0 + 2W_1 + W_2}{W_0 + 2W_1 + W_2 + W_1^0} \frac{S_0 - \langle S_z \rangle}{S_0} \frac{\gamma_S}{\gamma_I}$$

$$\varepsilon = 1 - \xi f s \frac{|\gamma_S|}{\gamma_I}$$

Coupling factor:  $\xi = \frac{W_2 - W_0}{W_0 + 2W_1 + W_2} = \frac{\sigma_{IS}}{\rho_I}$

Leakage factor:  $f = \frac{W_0 + 2W_1 + W_2}{W_0 + 2W_1 + W_2 + W_1^0} = \frac{\rho_I}{\rho_I + W_1^0}$

Saturation factor:  $s = \frac{S_0 - \langle S_z \rangle}{S_0}$

$$\frac{d}{dt} \begin{pmatrix} \langle I_z \rangle \\ \langle S_z \rangle \end{pmatrix} = - \begin{pmatrix} \rho_I & \sigma_{IS} \\ \sigma_{IS} & \rho_S \end{pmatrix} \begin{pmatrix} \langle I_z \rangle - I_0 \\ \langle S_z \rangle - S_0 \end{pmatrix}$$

$\rho$  = auto-relaxation rate       $\sigma$  = cross-relaxation rate



# Leakage factor

$$\varepsilon = 1 - \xi f_S \frac{|\gamma_S|}{\gamma_I}$$

- $f = \frac{W_0 + 2W_1 + W_2}{W_0 + 2W_1 + W_2 + W_1^0} = \frac{\rho_I}{\rho_I + W_1^0}, \quad 0 < f < 1$
- Defines proportion of nuclear relaxation caused by the paramagnetic electron
- Typically close to 1, unless low concentration of radical (small  $\rho_I$ ), or another very efficient source of relaxation (large  $W^0$ )

# Saturation factor

$$\varepsilon = 1 - \xi f_s \frac{|\gamma_s|}{\gamma_I}$$

- $s = \frac{S_0 - \langle S_z \rangle}{S_0}$ ,  $0 < s < 1$
- No saturation,  $\langle S_z \rangle = S_0$ ,  $s = 0$
- Full saturation,  $\langle S_z \rangle = 0$ ,  $s = 1$
- The greater the saturation, the larger the enhancement
- $s = 1 - \frac{1 + \Omega^2 T_{2e}^2}{1 + \Omega^2 T_{2e}^2 + \omega_{1e}^2 T_{1e} T_{2e}}$ ,  $\Omega = \omega_{\mu w} - \omega_{0s}$  (electron offset)  
 $\omega_{1e}$  = microwave power
- SQ transition is allowed, so less  $\mu w$  power required to saturate

# Coupling factor

$$\varepsilon = 1 - \xi f_S \frac{|\gamma_S|}{\gamma_I}$$

$$\bullet \xi = \frac{W_2 - W_0}{W_0 + 2W_1 + W_2} = \frac{\sigma_{IS}}{\rho_I}, \quad -1 < \xi < \frac{1}{2}$$

• Measures if ZQ or DQ relaxation dominates

•  $W_2 > W_0$ ,  $\xi > 1$ , negative enhancement

For positive  $\gamma_I$  !

•  $W_2 < W_0$ ,  $\xi < 1$ , positive enhancement

• Same sign rules as solid effect – but we can't choose ZQ or DQ

What determines the relaxation rates?

# Solomon Theory

- Hyperfine coupling Hamiltonian:  $\hat{H} = \hat{\mathbf{S}} \cdot \mathbb{A} \cdot \hat{\mathbf{I}}$
- Hyperfine coupling can have scalar (Fermi contact) and/or dipolar components:  $\mathbb{A} = A^{\text{FC}} + \mathbb{A}^{\text{dip}}$

# Solomon Theory – Fermi Contact

- Fermi contact is isotropic:
- $\hat{H} = A^{\text{FC}} \hat{\mathbf{I}} \cdot \hat{\mathbf{S}} = A^{\text{FC}} \left[ \hat{I}_z \hat{S}_z + \frac{1}{2} (\hat{I}_+ \hat{S}_- + \hat{I}_- \hat{S}_+) \right]$
- This can only induce ZQ relaxation ( $\hat{I}_+ \hat{S}_-$  and  $\hat{I}_- \hat{S}_+$  terms)
- $W_1 = W_2 = 0$ .  $\xi = \frac{-W_0}{W_0} = -1$ . Positive enhancement for positive  $\gamma_I$

$$\varepsilon = 1 - \xi f_s \frac{|\gamma_s|}{\gamma_I}$$

# Solomon Theory – Dipolar Coupling

- Dipolar coupling is anisotropic, giving SQ ( $\hat{I}_+ \hat{S}_z, \hat{I}_- \hat{S}_z$ ) and DQ terms ( $\hat{I}_+ \hat{S}_+, \hat{I}_- \hat{S}_-$ )

- $$\xi = \frac{W_2^{\text{dip}} - W_0^{\text{dip}}}{W_0^{\text{dip}} + 2W_1^{\text{dip}} + W_2^{\text{dip}}}$$

- Relaxation is driven by the spectral density of the fluctuating interactions at the transition frequency,  $J(\omega, \tau)$ , where  $\tau$  is the correlation time of the fluctuations.

$$W_0^{\text{dip}} = k_{\text{dip}} J(\omega_S - \omega_I, \tau_{\text{dip}})$$

$$W_1^{\text{dip}} = \frac{3}{2} k_{\text{dip}} J(\omega_I, \tau_{\text{dip}})$$

$$W_2^{\text{dip}} = 6 k_{\text{dip}} J(\omega_S + \omega_I, \tau_{\text{dip}})$$

# Solomon Theory

- Noting that  $\omega_S \gg \omega_I$ ,  $(\omega_S - \omega_I) \approx (\omega_S + \omega_I) \approx \omega_S$
- $$\xi = \frac{W_2^{\text{dip}} - W_0^{\text{dip}}}{W_0^{\text{dip}} + 2W_1^{\text{dip}} + W_2^{\text{dip}}} = \frac{5k_{\text{dip}}J(\omega_S, \tau_{\text{dip}})}{7k_{\text{dip}}J(\omega_S, \tau_{\text{dip}}) + 3k_{\text{dip}}J(\omega_I, \tau_{\text{dip}})}$$
- Spectral density is Lorentzian:  $J(\omega, \tau) = \frac{\tau}{1 + \omega^2 \tau^2}$

$$W_0^{\text{dip}} = k_{\text{dip}} J(\omega_S - \omega_I, \tau_{\text{dip}})$$

$$W_1^{\text{dip}} = \frac{3}{2} k_{\text{dip}} J(\omega_I, \tau_{\text{dip}})$$

$$W_2^{\text{dip}} = 6 k_{\text{dip}} J(\omega_S + \omega_I, \tau_{\text{dip}})$$

# Solomon Theory

- Noting that  $\omega_S \gg \omega_I$ ,  $(\omega_S - \omega_I) \approx (\omega_S + \omega_I) \approx \omega_S$
- $$\xi = \frac{W_2^{\text{dip}} - W_0^{\text{dip}}}{W_0^{\text{dip}} + 2W_1^{\text{dip}} + W_2^{\text{dip}}} = \frac{5k_{\text{dip}}J(\omega_S, \tau_{\text{dip}})}{7k_{\text{dip}}J(\omega_S, \tau_{\text{dip}}) + 3k_{\text{dip}}J(\omega_I, \tau_{\text{dip}})}$$
- Spectral density is Lorentzian:  $J(\omega, \tau) = \frac{\tau}{1 + \omega^2 \tau^2}$
- $\tau_{\text{dip}} \sim 10 - 100$  ps.
- At all reasonable fields,  $\omega_I \tau_{\text{dip}} \ll 1$ ,  $J(\omega_I, \tau_{\text{dip}}) = \tau_{\text{dip}}$
- Below a field of  $\sim 0.1$  T,  $\omega_S \tau_{\text{dip}} \ll 1$ ,  $J(\omega_S, \tau_{\text{dip}}) = \tau_{\text{dip}}$



# Solomon Theory

$$\varepsilon = 1 - \xi f_S \frac{|\gamma_S|}{\gamma_I}$$

$$\xi = \frac{5k_{\text{dip}}J(\omega_S, \tau_{\text{dip}})}{7k_{\text{dip}}J(\omega_S, \tau_{\text{dip}}) + 3k_{\text{dip}}J(\omega_I, \tau_{\text{dip}})}$$

$$J(\omega, \tau) = \frac{\tau}{1 + \omega^2\tau^2}$$

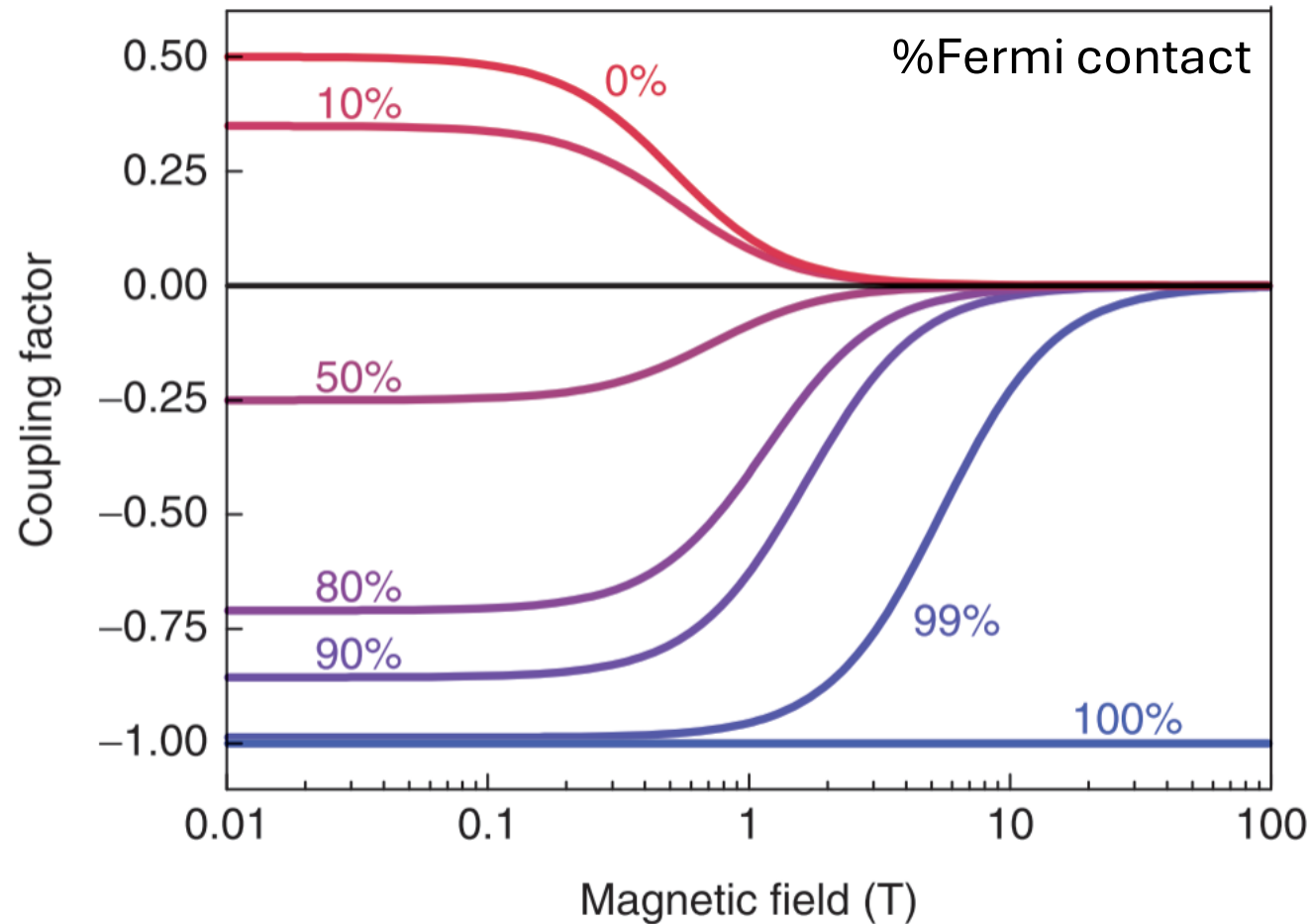
• At low field,  $J(\omega_S, \tau_{\text{dip}}) = J(\omega_I, \tau_{\text{dip}}) = \tau_{\text{dip}}$

•  $\xi = \frac{5k_{\text{dip}}\tau_{\text{dip}}}{10k_{\text{dip}}\tau_{\text{dip}}} = +\frac{1}{2}$ , negative enhancement for positive  $\gamma_I$

• At high field,  $\omega_S\tau_{\text{dip}} \gg 1$ ,  $J(\omega_S, \tau_{\text{dip}}) = \frac{1}{\omega_S^2\tau_{\text{dip}}} \ll J(\omega_I, \tau_{\text{dip}})$

•  $J(\omega_I, \tau_{\text{dip}})$  dominates,  $\xi \approx \frac{1}{3k_{\text{dip}}J(\omega_I, \tau_{\text{dip}})} \approx 0$

# Coupling factor field dependence



- Overhauser only works at high field if dominated by Fermi Contact (scalar)
- Any dipolar contribution will dominate at high enough field, suppressing the Overhauser effect.